

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ

فَاذْكُرُوا

**AIN SHAMS UNIVERSITY**  
**Faculty of Computer and Information Sciences**  
**Scientific Computing Department**



# **3D Object Retrieval**

Thesis submitted to the Department of Scientific Computing  
Faculty of Computer and Information Sciences  
Ain Shams University

In partial fulfillment of the requirements for the degree  
of Master of Computer and Information Sciences

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**Cairo - 2014**



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**“فخذ ما آتيتك وكن من الشاكرين”**

[سورة الأعراف - آية 144]

**“So take what I have brought you, and be of the thankful”**

[Al-A'raf – 144]

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# ***Dedication***

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# Abstract

*The advent of the World Wide Web as well as the rapid evolution in graphics hardware and software development, has given the opportunity to experience applications using 3D models not only to specialized users of the scientific community and the industrial domain, but also to common users. The number of available 3D models in digital libraries as well as domain-specific databases has increased substantially. 3D models are currently being used in a wide variety of vital fields. For example, the medical industry uses detailed 3D models of organs, the science sector uses 3D models as highly detailed models of chemical compounds, the architecture industry demonstrates proposed buildings and landscapes through Software Architectural 3D Models in addition to the engineering community which uses 3D models to design new devices, vehicles and structures. In recent decades the earth science community has also started to construct 3D geological models as a standard practice.*

*Though the number of 3D models keeps on increasing, 3D models are time and effort consuming to build. A more convenient and profitable approach is the use of existing 3D models instead of creating 3D models from scratch. Therefore, the challenge has shifted from “How can we generate 3D models?” to “How can we search 3D models?”*

*3D model search and retrieval could be performed by using a textual description of the user’s target which identifies the semantic meaning of the desired model or class of models. In this case, the user would explicitly describe the target, but such an approach is sensitive to the user’s subjectivity factor which is not necessarily in agreement with the textual information which has been annotated to the target. Furthermore, this method is problematic as it requires individually annotating every model of a repository which is impractical due to the huge and continuously increasing number of existing 3D models.*

*Therefore, content-based 3D object retrieval methods are suited for search since they do not require any annotation while. They only require robust 3D shape feature extraction that can be applied automatically. In these methods, a shape descriptor is computed which represents the model and is consequently used at the matching stage. When 3D model comparison is performed, it is required that shape descriptors are compact in size, discriminative as well as invariant under geometrical*

*transformations, deformations and possible perturbations. Thereafter, the discriminative power of these methods is highly affected by these aspects, while extraction and comparison time also affect the performance, especially for real-time applications.*

*Recently, a major effort of the research community has been devoted to the creation of accurate and efficient content based 3D object retrieval algorithms. Nevertheless, the problem remains challenging and it is far from being completely solved due to the lack of unique measure that defines shape similarity between 3D models. Work on shape representations and matching is based on a trade-off between conciseness and expensiveness of the chosen scheme.*

*In this thesis, we present a robust and efficient content-based 3D object retrieval technique after presenting a comprehensive survey of different methods proposed in literature. The key idea of the proposed technique is the synergy between Heat Kernel Signatures (HKS) (Sun et al., 2009) and Bag of Features (BoF) paradigm (Harris, 1954), such that the problem of matching different 3D models is reduced to simply matching their corresponding bags of features vectors which act as their representative shape descriptors. First, the HKS computation phase encodes each point in a given 3D model by a feature vector describing its local and global geometric properties at different time values. Next during the feature point detection and description phase, HKS critical points are captured in order to constitute an initial set of feature points. Then, an innovative filtering technique is applied on this initial set in order to carefully pick the most stable significant feature points, resulting in a compact set of points covering the whole surface of a given 3D model uniformly. This concise set of feature points constitutes the final feature space required for constructing the geometric vocabulary that holds the most distinct geometric words. It should be pointed out that, each point belonging to such descriptor space is associated with a compact and informative HKS-based feature descriptor vector. Afterwards through the BoF phase, each point from a given 3D model is associated to the nearest visual word in the given geometric vocabulary, which has been preliminary built using K-means clustering technique in the descriptor space. Then, the 3D model is represented by a BoF distribution representing a histogram of occurrences of the visual words all over the model. Eventually, the problem of matching 3D models is reduced to matching their corresponding significant BoF descriptors.*

*Through our extensive evaluation experiments, we conclude that the proposed technique is quite effective for the purpose of 3D Object Retrieval, showing very high*



*retrieval accuracy and descriptive power. It achieves state of the art results on SHREC 2011 dataset; a public well known benchmark of non-rigid 3D models. The proposed descriptor is not only invariant against different kinds of deformations and transformations, but also can handle 3D models under perturbations of noise. Moreover, it is significant that the proposed technique is computationally efficient.*

*Furthermore, we compare the proposed technique with other state of the art methods recently proposed in literature. The proposed technique clearly outperforms all other competitive methods, providing quite good results almost always better than other methods regarding different standard evaluation metrics.*

*In conclusion, the significant contributions of our work can be summarized in introducing a compact, easily computed and informative HKS-based feature vector for point feature description, applying a robust filtering technique for reducing time and space complexity of clustering descriptor space required for geometric vocabulary construction, encoding 3D models with a compact highly discriminative feature descriptor and finally attaining high retrieval results invariant against noise and different kinds of both deformations and transformations.*

*In the future, we look forward to exploring other applications in the area of 3D shape analysis. In addition to adapting our technique so that it can be applied in other 3D applications such as partial matching, segmentation, pose estimation and matching specific domain 3D models.*

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