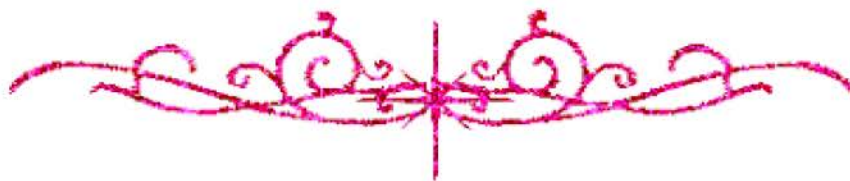


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شبكة المعلومات الجامعية التوثيق الالكتروني والميكروفيلم



جامعة عين شمس

التوثيق الإلكتروني والميكروفيلم

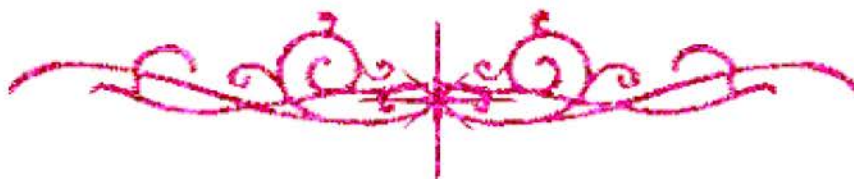
قسم

نقسم بالله العظيم أن المادة التي تم توثيقها وتسجيلها
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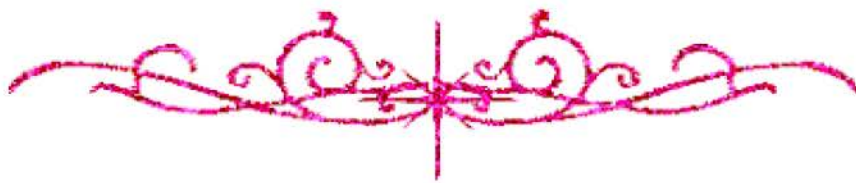
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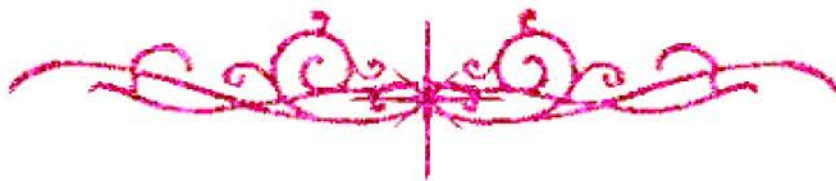


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CAIRO UNIVERSITY
FACULTY OF ECONOMICS AND POLITICAL SCIENCES
DEPARTMENT OF STATISTICS

STATISTICAL-RELIABILITY ANALYSIS FOR REPAIRABLE SYSTEMS

By

FATMA HASSAN EL-ZANATY

A Thesis Submitted in Accordance with the
Regulations for Candidate for Ph.D. Degree
In Statistics

1986

احياء, sheet

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REPAIRABLE SYSTEMS

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REPAIRABLE SYSTEMS

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in Statistics has been approved by:

Three handwritten signatures in blue ink, each on a horizontal line. The signatures are stylized and appear to be in Arabic script.

TABLE OF CONTENTS

Chapter		Page
I	INTRODUCTION.	1
II	REVIEW OF RELATED LITERATURE.	8
	2.1. Introduction	8
	2.2. Repairable Systems With Standbys	9
	2.3. The K-out-of-n System With Repair.	15
III	AVAILABILITY AND RELIABILITY ANALYSIS FOR A REPAIRABLE SYSTEM WITH N-UNITS AND M-STANDBY. . .	20
	3.1. Introduction	20
	3.2. Difference-Differential Equations for the System	20
	3.3. Solution to the Difference-Differential Equations in Case $N=1$ and $M=1$	23
	3.3.1. Availability of the system.	25
	3.3.2. Reliability of the system	27
	3.4. Solution to the Difference-Differential Equations in Case $N=2$ and $M=1$	30
	3.4.1. Case (1): real roots.	32
	3.4.2. Case (2): equal roots	40
	3.4.3. Case (3): imaginary roots	55
	3.4.4. Reliability of the system	72

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Chapter	Page
IV	
AVAILABILITY AND RELIABILITY OF K-OUT-OF-n	
SYSTEMS	81
4.1. Introduction	81
4.2. Availability and Reliability of the	
K-out-of-n System (Case $N=1$ and $M=1$)	81
4.2.1. Reliability of the K-out-of-n	
System ($N=1, M=1$)	91
4.3. Availability and Reliability of the K-out-	
of-n System (case $N=2$ and $M=1$).	102
4.3.1. Case of real roots ($0.8989794 < \rho \leq 1$)	103
4.3.2. Case of equal roots $\rho = 0.8989794$).	110
4.3.3. Case of imaginary roots	
($0 < \rho < 0.8989794$).	119
4.3.4. Reliability of the K-out-of-n	
system.	131
4.4. Conclusions.	144
REFERENCES.	146

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LIST OF FIGURES

Figure	Page
(3.1): $P_1(t)$ and $P_0(t)$ for $\tau_1=0.75$, and $\rho=0.1, 0.09$ (case $N=1, M=1$)	26
(3.2): $P_1(t)$ and $P_0(t)$ for $\rho = 0.1, 0.9$ (case of reliability).	29
(3.3): $P_0(t), P_1(t)$ and $P_2(t)$ for $\tau_1=0.2, \tau_2=0.65, \rho=0.95$ $A_1=0.1333 > 0, A_2=0.2083 > 0$ (case of real roots)..	42
(3.4): $P_0(t), P_1(t)$ and $P_2(t)$ for $\tau_1=0.2, \tau_2=0.75, \rho=0.9$ and $A_1=-1.6136 < 0, A_2=2.0465 > 0$ (case of real roots). . . .	43
(3.5): $P_0(t), P_1(t)$ and $P_2(t)$ for $\tau_2=0.6, \tau_1=0.2, \rho=0.9$ and $A_1=0.6364 A_2=-0.3536$ (case of real roots). . . .	44
(3.6): $P_0(t), P_1(t)$ and $P_2(t)$ for $\tau_2=0.7$ and $\tau_1=0.2$ (case of equal roots).	53
(3.7): $P_2(t)$ for $\rho=0.3 \tau_2=0.7$ (case of imaginary roots) .	58
(3.8): $P_1(t)$ for $\rho=0.5$, and $\tau_1=0.2$ (case of imaginary roots).	60
(3.9): $P_0(t)$ for $\rho=0.5$ (case of imaginary roots). . . .	63
(3.10): $P_0(t), P_1(t)$ and $P_2(t)$ for $\tau_2=0.7, \tau_1=0.3$ and $\rho=0.5$ $A_1 > 0, A_2 > 0$ (case of reliability).	79
(3.11): $P_0(t), P_1(t)$ and $P_2(t)$ for $\tau_2=0.6, \tau_1=0.4$ and $\rho=0.1$ $A_1=-0.3881, A_2=0.9881$ (case of reliability). . . .	80

Figure	Page
(4.1) : Availability of the 1-out-of-3 system or $\tau_1=0.75$ and $\rho=0.3, 0.8$	84
(4.2) : Availability of the 2-out-of-4 system for $\rho=0.5$ and $\tau_1=0.75, 0.9$	85
(4.3) : Availability of the K-out-of-5 system for $\tau_1=0.7,$ $\rho=0.6$ and $K=1, 5$	87
(4.4) : Availability of the 3-out-of-n system for $\rho=0.1,$ $\tau_1=0.9$ and $n = 5,10$	88
(4.5) : Availability of the parallel system for $\tau_1=0.8,$ $\rho=0.5$ and $n = 3, 5$	90
(4.6) : Availability of the series system for $\tau_1=0.8,$ $\rho=0.5$ and $n = 5,10$	92
(4.7) : Reliability of the 2-out-of-5 system for $\rho=0.1, 0.9$	94
(4.8) : Reliability of the parallel system for $\rho=0.9$ and $n = 3,5$	96
(4.9) : Reliability of the series system for $\rho=0.5$ and $n = 4,10$	98
(4.10): Reliability of the K-out-of-4 system for $\rho=0.5$ and $K=1, 3$	99
(4.11): Reliability of the 2-out-of-n system for $\rho=1$ and $n=5,8$	101

Figure	Page
(4.12): Availability of the 2-out-of-4 system for $\rho = 1$, $\pi_1 = 0.2$ and $\pi_2 = 0.6, 0.75$. $N=2, M=1$ (case of real roots)	105
(4.13): Availability of the 4-out-of-6 system for $\rho = 0.95$, $\pi_2 = 0.65$ and $\pi_1 = 0.2, 0.3$ (case of real roots)	107
(4.14): Availability of the 2-out-of-6 system for $\pi_1 = 0.2$ $\pi_2 = 0.7$ and $\rho = 0.9, 1.0$ (case of real roots)	108
(4.15): Availability of the series system for $\rho = 0.95$, $\pi_1 = 0.2$ $\pi_2 = 0.7$ and $n=4, 8$ (case of real roots)	111
(4.16): Availability of the parallel system for $\rho = 0.9$, $\pi_1 = 0.2$, $\pi_2 = 0.75$ and $n=6, 10$ (case of real roots)	112
(4.17): Availability of the 3-out-of- n system for $\rho = 0.9$, $\pi_1 = 0.2$ $\pi_2 = 0.6$ and $n=6, 8$ (Case of real roots)	114
(4.18): Availability of the 2-out-of-4 system for $\pi_1 = 0.2$ and $\pi_2 = 0.6, 0.75$ (case of equal roots)	116
(4.19): Availability of the 4-out-of-6 system for $\pi_2 = 0.65$ and $\pi_1 = 0.2, 0.3$ (case of equal roots)	118
(4.20): Availability of the series system for $\pi_1 = 0.2$, $\pi_2 = 0.65$ and $n=4, 8$ (case of equal roots)	120
(4.21): Availability of the parallel system for $\pi_1 = 0.2$, $\pi_2 = 0.7$ and $n=6, 10$ (case of equal roots)	122
(4.22): Availability of the 4-out-of- n system for $\pi_1 = 0.2$ $\pi_2 = 0.6$ and $n=6, 10$ (case of equal roots)	123

Figure	Page
(4.23): Availability of the 3-out-of-4 system for $\pi_1=0.2$ $\pi_2=0.6$ and $\rho=0.1, 0.8$ (case of imaginary roots). . .	126
(4.24): Availability of the 3-out-of-6 system for $\rho=0.5$, $\pi_1=0.2$ and $\pi_2=0.6, 0.75$ (case of imaginary roots)...129	
(4.25): Availability of the parallel system for $\rho=0.5$, $\pi_1=0.2$, $\pi_2=0.7$ and $n=4, 8$ (case of imaginary roots).130	
(4.26): Availability of the series system for $\rho=0.1$, $\pi_1=0.2$, $\pi_2=0.65$ and $n=6, 10$ (case of imaginary roots).. . .	132
(4.27): Availability of the 5-out-of-n system for $\rho=0.5$ $\pi_1=0.2$, $\pi_2=0.6$ and $n=6, 8$ (case of imaginary roots)..134	
(4.28): Reliability of the 4-out-of-n system for $\pi_1=0.2$, $\pi_2=0.8$ and $\rho=0.5, 1.0$	136
(4.29): Reliability of the 3-out-of-6 system for $\rho=0.5$ and $\pi_2=0.55, 0.75$	138
(4.30): Reliability of the parallel system for $\rho=0.1$, $\pi_1=0.3$ $\pi_2=0.7$ and $n=4, 8$	139
(4.31): Reliability of the series system for $\rho=0.5$, $\pi_1=0.3$ $\pi_2=0.7$ and $n=6, 10$	141
(4.32): Reliability of the 3-out-of-n system for $\rho=0.1$, $\pi_1=0.4$ $\pi_2=0.6$ and $n=4, 8$	142

LIST OF TABLES

Table	Page
(4.1) : Availability of the 1-out-of-3 system for $\pi_1=0.75$ and $\rho=0.3,0.8$	86
(4.2) : Availability of the 2-out-of-4 system for $\rho=0.5$ and $\pi_1=0.75,0.9$	86
(4.3) : Availability of the K-out-of-5 system for $\pi_1=0.7$, $\rho=0.6$ and $K=1,5$	89
(4.4) : Availability of the 3-out-of-n system for $\rho=0.1$, $\pi_1=0.9$ and $n=5,10$	89
(4.5) : Availability of the parallel system $\pi_1=0.8, \rho=0.5$ and $n=3,5$	93
(4.6) : Availability of the series system for $\pi_1=0.8$, $\rho=0.5$ and $n=5,10$	93
(4.7) : Reliability of the 2-out-of-5 system for $\rho=0.1,0.9$	97
(4.8) : Reliability of the parallel system for $\rho=0.9$ and $n=3,5$	97
(4.9) : Reliability of the series system for $\rho=1$ and $n=4,10$	100
(4.10) : Reliability of the K-out-of-4 system for $\rho=0.5$ and $K=1,3$	100
(4.11) : Reliability of the 2-out-of-n system for $\rho=1$, and $n=5,8$	106