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Science and Education
Ain Shams University

ELECTRON TRANSPORT PROPERTIES IN SEMICONDUCTOR AT HIGH ELECTRIC FIELDS

By

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In the name of Allah, most gracious, most merciful.

“And say: Work (righteousness): Soon will Allah observe your work, and his messenger and the believers “

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