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شبكة المعلومات الجامعية

التوثيق الالكتروني والميكروفيلم

شبكة المعلومات الجامعية

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التوثيق الالكتروني والميكروفيلم

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Study and Developing Some Subjects in Complex Analysis

A THESIS

Submitted to Faculty of Science
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For the Degree of Doctor of Philosophy in Science
(Mathematics - Complex Analysis)

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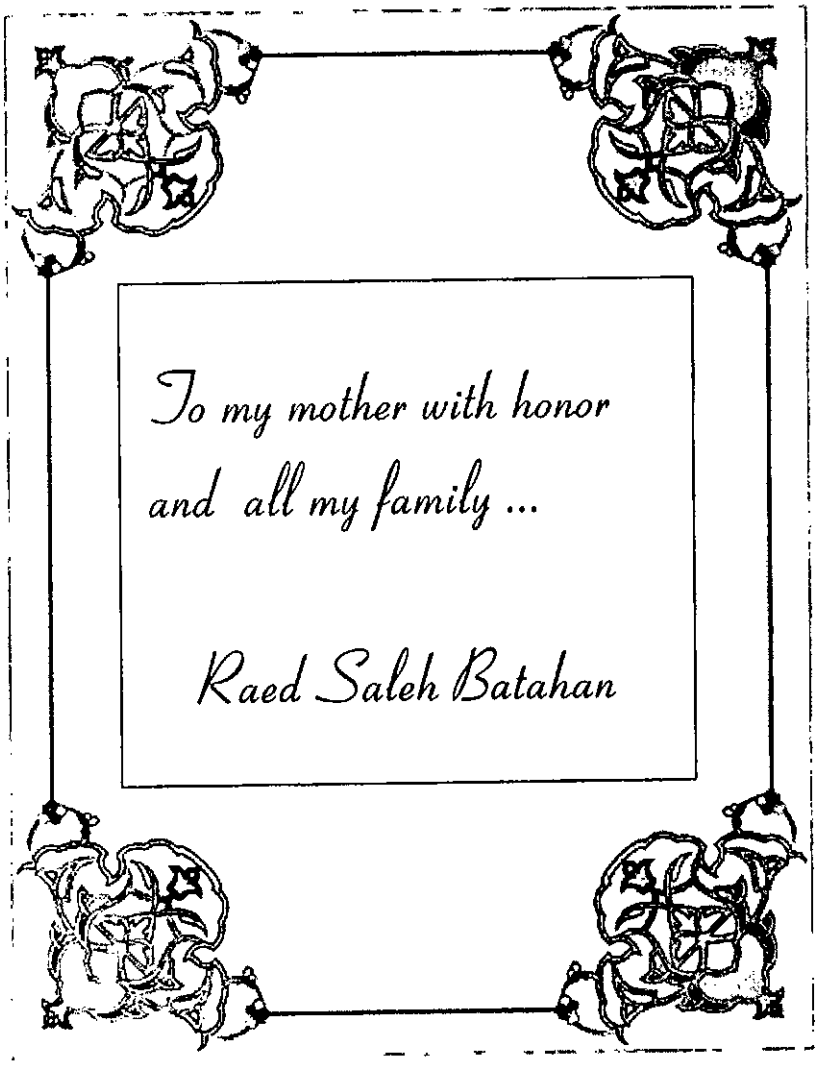
To my mother with honor
and all my family ...
Raed Saleh Batahan

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