



***A Theoretical Study of Digital Filters
and
Its Applications in Some Physical Phenomena***

Thesis

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SUMMARY

