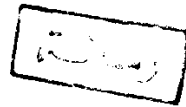


EFFICIENT ALGORITHMS FOR THE
LINEAR DECONVOLUTION PROBLEM
IN SEISMIC DATA PROCESSING

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O.M.

Ph.D. THESIS
(GEOPHYSICS)



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59139

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1997





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**Ph.D. THESIS
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