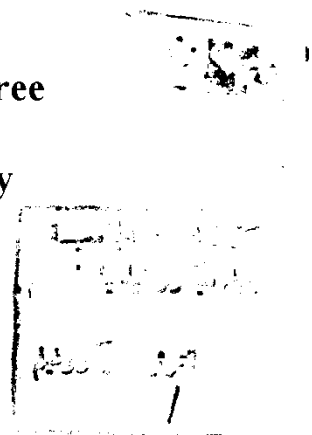


**EXISTENCE, FORMATION AND ANNIHILATION
OF HYDROGEN - ANTIHYDROGEN MOLECULES**



Thesis
Submitted for the degree
of
Doctor of Philosophy
in
Physics



539.6
E. A

To
Physics Department
Faculty of Science
Ain Shams University

64188

Handwritten signature in Arabic script.

By
Esraa Ali Ahmad El- Khateeb
B.Sc. 1986
M.Sc. 1990

Handwritten signature in Arabic script.

1995

Handwritten signature in Arabic script.



بسم الله الرحمن الرحيم

"وأخر دعوانهم أن الحمد لله رب العالمين"

صدق الله العظيم

To my Father

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