EXISTENCE, FORMATION AND ANNIHILATION OF HYDROGEN - ANTIHYDROGEN MOLECULES

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" وآخر دعواهم أن الحمد لله رب العالمين "

صدق الله العظيم

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To my Father

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ACKNOWLEDGEMENT

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