THEORETICAL AND EXPERIMENTAL INVESTIGATIONS OF THERMAL CONDUCTIVITY OF PLAIN AND REINFORCED CONCRETE WITH APPLICATION TO WATER TANKS

THESIS

SUBMITTED FOR THE DEGREE OF DOCTOR OF PHILOSOPHY
IN
CIVIL ENGINEERING

BY

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Theoretical and Experimental Investigations of Thermal Conductivity of Plain and Reinforced Concrete With Application to Water Tanks.

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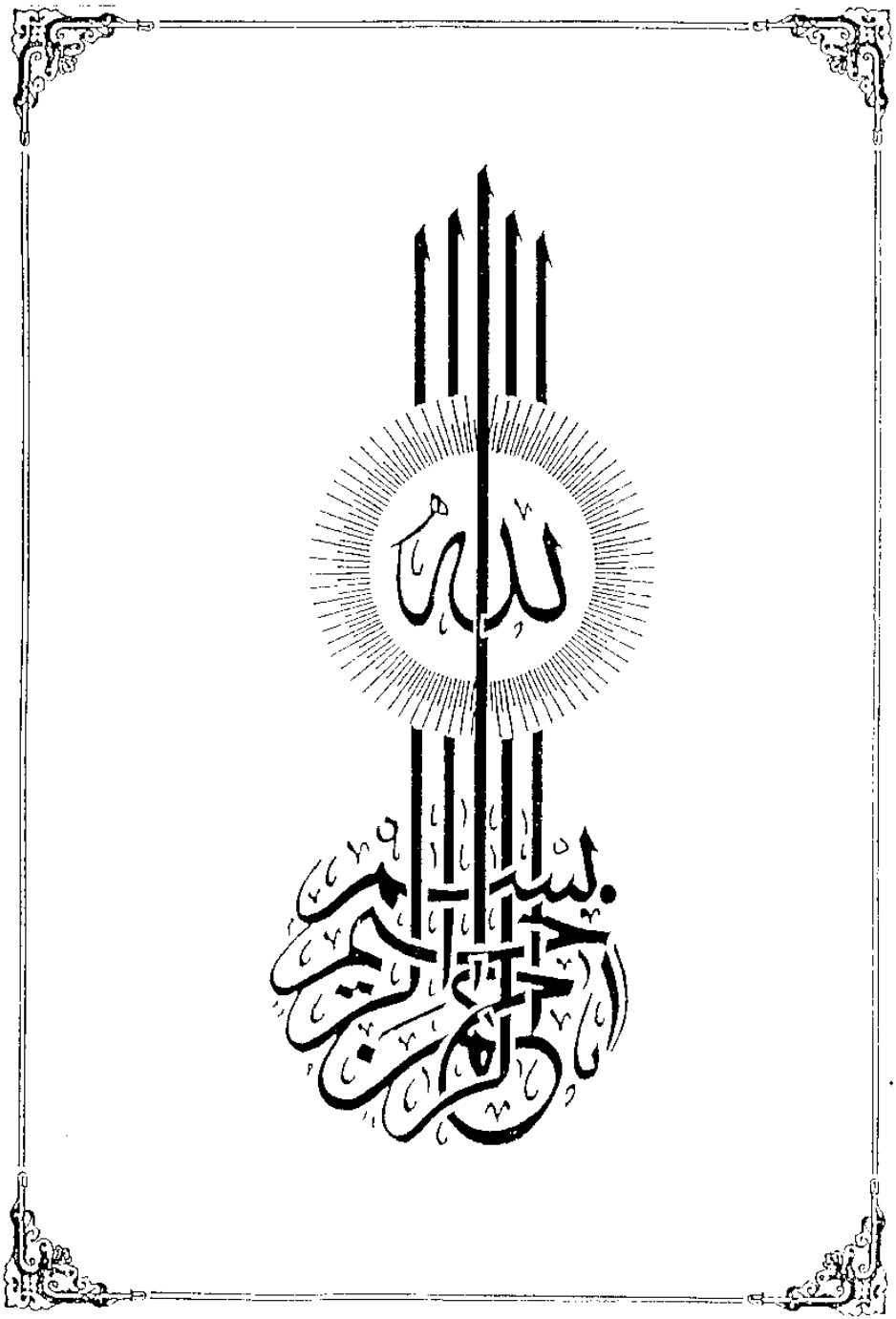

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ACKNOLEDGEMENT

The author wishes to express her deep gratitude and sincere appreciation to **Dr. Abd El-Kerim Atta,** Professor of strength of materials, Faculty of Engineering, Ain-Shams University for his guidance, generous supervision and continuous encouragement which have greatly contributed in achieving this work.

The author wishes to express her deep thanks to **Dr. Mohamed Salah El-Hoary,** Head of Public Work Department, Faculty of Engineering, Ain-Shams University for his sincere help.

Special thanks to **Dr. Ezzat Hashem Morsy,** Prof. of strength of materials, General Organization of Housing, Building and Planning Research for his help and facilities given to carry out this work. Thanks are also to the staff of strength of materials laboratory for their help.

The author is appreciated to **Dr. George Bassili Hanna,** Prof. of building physics, General Organization of Housing, Building and Planning Research for his guidence and encouragement during this work. Appreciation is also extend to his staff of Building Physics Laboratory.

Thanks are also given to **Dr. Abou Zeid Rageh,** Chairman of General Organization of Housing, Building and Planning Research for his encouragement.

Finally, the author would like to acknowledge the encouragement and support shown by her mother and her husband.

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