



Some Hydrodynamic Problems with Moving **Boundary Conditions**

Thesis

Submitted in Partial Fulfillment for the Requirement of the Master Degree in Teacher Preparation in Science (Applied Mathematics)

To

Department of Mathematics Faculty of Education-Ain Shams University

By

Mohamed Hassan Haroun Hassan,

Demonstrator of Dept. of Mathematics, Faculty of Education- Ain Shams University, B.Sc. & Education (Mathematics-1992).

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Under Supervision of

Prof. Dr. El-Sayed F. El-Shehawey,

Head of the Department of Mathematics, ...y of Education, Ain Shams University.

1998

Dr. H. E. Gad -Allah,

Lecturer of Mathematics, Faculty of Education, Ain Shams University.





TO ALL MY FAMILY

Acknowledgements

<u>Acknowledgements</u>

I am deeply thankful to Allah, who always helps and guides me.

I would like to express my deepest gratitude and special thanks to **Prof. Dr. El-Sayed F. El-Shehawey**, Head of the Department of Mathematics, Faculty of Education, Ain Shams University, for suggesting the points, helpful guidance and for offering me valuable facilities during the supervision of this thesis

I would like to express my deepest gratitude to **Dr. H. Gad-Allah**, Lecturer of Mathematics, Faculty of Education,

Ain Shams University for his kind supervision and cooperation.

Finally, many thanks to the staff of the Department of Mathematics, Faculty of Education, Ain Shams University, specially **Dr. Elsayed M. E. Elbarbary**, for their continuous encouragement.

Contents

			Page
Chapter	I	PrefaceIntroduction	I 1
	1.1	Development of Fluid Mechanics	1
	1.2	Newtonian and Non-Newtonian Fluids	7
	1.3	Travelling and Standing Waves	8
	1.4	Free, Moving and Mixed-Boundary Value Problems	8
	1.5	Dimensions and Units	10
	1.6	Reynolds Number and Froude Number	13
	1.7	On Two-Phase Flow	14
	1.8	On Virtual Mass	16
	1.9	On Perturbation Method	17
	1.10	The Human Ureter	19
	1.11	The Peristalsis in Small Intestine	20
	1.12	The Basic Equations for a Pure Fluid	24
	1.13	The Basic Equations for a Two-Phase Flow	26
Chapter	11	The Effect of Virtual Mass on Peristaltic Transport of a Particle-Fluid Suspension	28
	2.1	Introduction	28
	2.2	Exampletion of the Broblem	30

	2.3	Method of Solution	37
	2.4	Free Pumping (Originally Stationary Fluid)	43
	2.5	Numerical Results and Discussions	46
Chapter	Ш	Peristaltic Pumping of a Fluid in an Inclined Planer Channel	72
	3.1	Introduction	72
	3.2	Formulation of the Problem	73
	3.3	Method of Solution.	76
	3.3.1	Closed Form Solutions for Small Values of Re and K1	79
	3.3.2	Method of Solution for Arbitrary Values of Re and K1	83
	3.4	Numerical Results and Discussions	86
		References	110

Preface

