

شبكة المعلومات الجامعية







شبكة المعلومات الجامعية التوثيق الالكتروني والميكروفيلم



شبكة المعلومات الجامعية

# جامعة عين شمس

التوثيق الالكتروني والميكروفيلم

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# بالرسالة صفحات لم ترد بالإصل



# A Study Of Some Efficient Algorithms For Drawing Graphs

ZX.CP

A Thesis

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Ву

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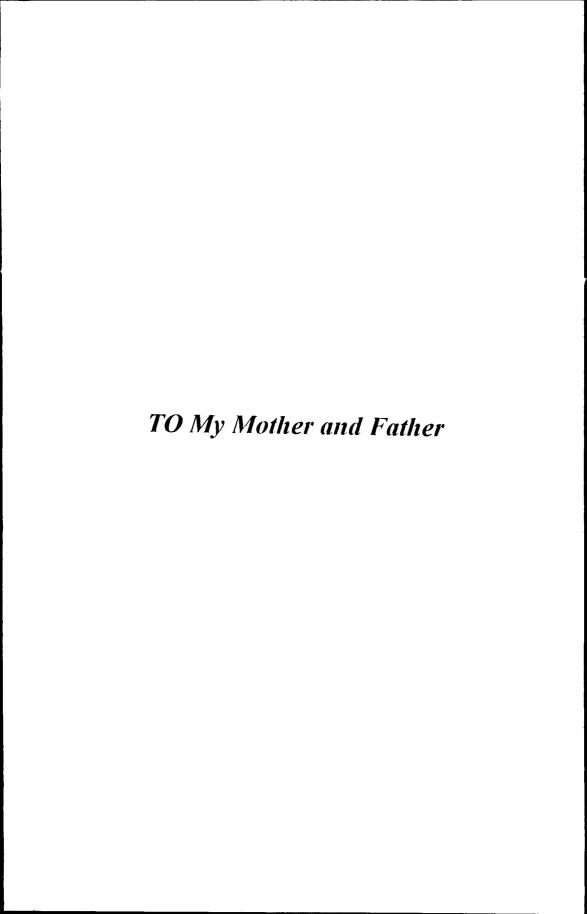
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