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A Study Of Some Efficient Algorithms For Drawing Graphs

27.5
UP

A Thesis

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(2002)

TO My Mother and Father



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