



AIN SHAMS UNIVERSITY
FACULTY OF ENGINEERING
Electronics and Communications Engineering Department

**Timing and frequency offset correction of received OFDM
symbols in advanced communication systems.**

A Thesis

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STATEMENT

This dissertation is submitted to Ain Shams University for the degree of Master of Science in Electrical Engineering (Electronics and Communications Engineering).

The work included in this thesis was carried out by the author at the Electronics and Communications Engineering Department, Faculty of Engineering, Ain Shams University, Cairo, Egypt.

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ABSTRACT

Marriam Abou Baker Mohammed

Timing and frequency offset correction of received OFDM symbols in advanced communication systems.

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This thesis presents a study of how to correct timing and frequency offset of orthogonal division multiplexing (OFDM). OFDM is considered the most common digital modulation technique in advanced communication systems such as ADSL, WLAN and Wi- MAX. OFDM systems have a great immunity against multipath fading, noise and any delayed channels.

Timing errors during transmission complicates the process of determining the start of the received OFDM symbol. In addition to some sort of phase rotation according to Fourier transform which translates the time delay into phase shift. Beside timing errors due to transmission, OFDM symbols may suffers from carrier frequency offsets due to multipath fading. Some old methods are used to solve the problem of synchronization such as 'data aided'.

This method uses predetermined training symbols which reduce the efficiency of transmitted channels due to the reduction of the part of band width dedicated for data transmission. A new method for synchronization depends on the cyclic prefix (CP) which is the process of copying the last L part of transmitted OFDM symbols to the beginning of OFDM symbol. CP represents a percentage of OFDM symbol. The effect of different percentages of CP in the synchronization process is tested.

MATLAB SIMULINK and HDL code generation is used for OFDM system simulation and HDL code generation.

Key words: OFDM (Orthogonal frequency division multiplexing) – CP (Cyclic prefix)- Timing errors –MTLAB-MATLAB HDL coder-timing synchronization.

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List of Abbreviations

WBMSC	Wireless Broad Band Multimedia Communication System
Mbps	Mega Bits Per Second
ISI	Inter Symbol Interference
OFDM	Orthogonal Frequency Division Multiplexing
FDM	Frequency Division Multiplexing
IEEE	Institute of Electrical and Electronics Engineering
WLAN	Wireless Local Area Network
MBWA	Mobile Broadband Wireless Access
GHZ	Giga hertz
ADSL	Asymmetric Digital Subcarrier Line
DAB	Digital Audio Broadcasting
MAC	Media Access Control
PHY	Physical layer
PLCP	Physical Layer Convergence Protocol
PSDU	Payload
BPSK	Binary Phase Shift Keying
WMAN	Wireless Metropolitan Area Network
BWA	Broadband Wireless Access
MIMO	Multiple Input Multiple Output
QoS	Quality of Service
LOS	Line of Site
NLOS	Non Line Of Site
QPSK	Quadrature Phase Shift Keying
QAM	Quadrature Amplitude Modulation
FFT	Fast Fourier Transform
IFFT	Inverse Fast Fourier Transform

CP	Cyclic Prefix
RF	Radio Frequency
TDMA	Time Division Multiple Access
FDMA	Frequency Division Multiple Access
CDMA	Code Division Multiple Access
OFDMA	Orthogonal Frequency Division Multiple Access
DFT	Discrete Fourier Transform
BER	Bit Error Rate
ICI	Inter Carrier Interference
ZP	Zero Prefix
WiMAX	Worldwide Interoperability for Microwave Access
SNR	Signal to Noise Ratio
CIR	Channel Impulse Response
PN	Pseudo Number
DAB	Digital Audio Broadcasting
DVB-T	Digital Video Broadcasting
MLE	Maximum Likelihood Estimation
AWGN	Additive White Gaussian Noise
DA	Data Aided
NDA	Non Data Aided
CFO	Carrier Frequency Offset
HDL	Hardware Description Language
FPGA	Field Programmable Gate Array
RS	Reed Solomon

List of symbols

T_s	Sampling time
t	Channel delay spread
L	Number of lower rate sub-streams
B_c	Coherent bandwidth
T_b	Original bit rate
B	Bandwidth of single carrier transmission
T_g	Guard band time interval
h	Channel impulse response
σ^2	Noise power
N	Total number of points processed by DFT or IDFT
n	Sample index of carrier
k	Number of cycles of N points
R	High data rate stream
τ	Timing offset
T_m	Maximum channel delay spread
N_g	Number of samples in guard interval
r_m	The received OFDM signal
$C(n)$	Cross correlation values
D	The amount of delay through transmission
$P(n)$	The received signal energy
$M(n)$	Timing metric
δf	Carrier frequency offset
Δf	Frequency spacing
$f(t)$	Signal in time domain
$F(f)$	Signal in frequency domain
f_s	Sampling frequency
θ	Phase shift