بسم الله الرحمن الرحيم

شبكة المعلومـــــات الجامعية

التوثيق الالكتروني والميكروفيلم

شبكة المعلومات الجامعية

جامعة عين شمس

التوثيق الالكتروني والميكروفيلم

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لم ترد بالأصـــل

Cairo University
Faculty of Engineering

Enhancements to Low Density Parity Check (LDPC) codes

By

Khaled AbdElKhalik ElSayed ElMahgoub

A Thesis Submitted to the
Faculty of Engineering at Cairo University
in Partial Fulfillment of the
Requirements for the Degree of
Master of Science
in
Electronics and Electrical Communications Engineering

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