



# A COMPARATIVE STUDY OF DIFFERENT CONTROL TECHNIQUES FOR ACTIVE SUSPENSION SYSTEMS

By

## Rana Mohamed Abdel Rahman Saleh

A Thesis Submitted to the

Faculty of Engineering at Cairo University

In Partial Fulfillment of the

Requirements for the Degree of

## **MASTER OF SCIENCE**

In

### ELECTICAL POWER AND MACHINES ENGINEERING

FACULTY OF ENGINEERING, CAIRO UNIVERSITY GIZA, EGYPT 2018

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Under the Supervision of

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Title of Thesis: A COMPARATIVE STUDY OF DIFFERENT CONTROL

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**Keywords:** Active Suspension, Fuzzy, PID, Particle Swarm Optimization, Feedback

Linearization

**Summary:** 

This research focuses on implementing a group of control techniques to enhance the performance of Active Suspension System for different vehicle's models under the presence of various road profiles.

Linear and nonlinear mathematical models of quarter and half vehicle and a linear model of full vehicle are presented. PID controller is used for the linear models and Feedback Linearization control is used for the nonlinear models whereas Fuzzy Logic controller is used for both the linear and nonlinear models. Particle Swarm Optimization is the tuning method for the provided controllers.

MATLAB/SIMULINK software is used for simulation which is based on the mathematical models. A comparison between the behavior of passive and active suspensions is demonstrated. Active suspension shows a significant enhancement compared to passive suspension.



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# **NOMENCLATURE**

### Acronyms

ASS Active Suspension System

HVASS Half Vehicle Active Suspension System

HVSS Half Vehicle Suspension System

PID Proportional Integral Derivative

PSO Particle Swarm Optimization

PSS Passive Suspension System

QVASS Quarter Vehicle Active Suspension System

QVSS Quarter Vehicle Suspension System

RMS Root Mean Square

### **Greek Symbols**

lpha Factor Depends on the road surface rad/s  $heta_s$  Pitch Angle of Sprung Mass rad

 $\rho$  Relative degree of the output signal w.r.t the disturbance signal

Roman Symbols

A Gaussian White Noise

*c*<sub>1</sub> Individual Weight

*c*<sub>2</sub> Sociality Weight.

 $C_s$  Suspension Damping Coefficient N.s/m

C<sub>sf</sub> Front Suspension Damping Coefficient N.s/m

 $C_{sr}$  Rear Suspension Damping Coefficient N.s/m

 $C_t$  Tire Damping Coefficient N.s/m

d Problem Dimensions

e Error Signal

| $h$ , $h_1$ , and $h_2$ | Bump Height  | m             |
|-------------------------|--|---------------|
| i                       | Number of iterations   |               |
| $I_s$ $K_d$             | Pitch moment of inertia Derivative Gain  | Kg            |
| $K_i$                   | Integral Gain  |               |
| $K_{ls}$ $K_{ns}$       | Linear Component of Suspension Stiffness Coefficient<br>Nonlinear Component of Suspension Stiffness<br>Coefficient             | $N/m$ $N/m^3$ |
| $K_p$                   | Proportional Gain  |               |
| $K_s$                   | Suspension Stiffness Coefficient   | N/m           |
| $K_{sf}$                | Front Suspension Stiffness Coefficient   | N/m           |
| $K_{sf}^{\ nl}$         | Front Suspension Nonlinear Stiffness Coefficient   | $N/m^3$       |
| $K_{sr}$                | Rear Suspension Stiffness Coefficient  | N/m           |
| $K_{sr}^{\ nl}$         | Rear Suspension Nonlinear Stiffness Coefficient  | $N/m^3$       |
| $K_t$                   | Tire Stiffness Coefficient   | N/m           |
| $K_{tf}$                | Front Tire Stiffness Coefficient   | N/m           |
| $K_{tr}$                | Rear Tire Stiffness Coefficient  | N/m           |
| L                       | Distance between the axle  | m             |
| $L_{I}$                 | Distance from Front Suspension Location to C.G. of<br>the Sprung Mass<br>Distance from Rear Suspension Location to C.G. of the | m             |
| $L_2$                   | Sprung Mass  | m             |
| $M_s$                   | Sprung Mass  | Kg            |
| $M_s$                   | Sprung Mass  | Kg            |
| $M_t$                   | Unsprung Mass  | Kg            |
| $M_{tf}$                | Front Unsprung Mass  | kg            |
| $M_{tr}$                | Front Unsprung Mas   | Kg            |
| $p_{gd}$                | Particle's Global Best Solution  |               |
| Pid                     | Particle's Local Best Solution   |               |
| r                       | Relative degree of the output signal w.r.t the input signal  |               |