



شبكة المعلومات الجامعية

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ



شبكة المعلومات الجامعية  
@ ASUNET



شبكة المعلومات الجامعية

# جامعة عين شمس

التوثيق الالكتروني والميكرو فيلم

## قسم

نقسم بالله العظيم أن المادة التي تم توثيقها وتسجيلها  
علي هذه الأفلام قد أعدت دون أية تغيرات



## يجب أن

تحفظ هذه الأفلام بعيدا عن الغبار

في درجة حرارة من 15-25 مئوية ورطوبة نسبية من 20-40%

To be Kept away from Dust in Dry Cool place of  
15-25- c and relative humidity 20-40%





# شبكة المعلومات الجامعية التوثيق الالكتروني والميكروفيلم

# **A STUDY OF BURR FAMILY OF DISTRIBUTIONS**

**THESIS**

**SUBMITTED IN PARTIAL FULFILLMENT  
OF THE REQUIREMENTS  
OF THE AWARD  
OF THE (M.Sc.) DEGREE  
(STATISTICS)**

**PRESENTED BY**

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**Supervised By**

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Department of Mathematics  
Faculty of Science, Ain Shams University

**SUBMITTED TO**

**Department of Mathematics  
Faculty of Science  
Ain Shams University**

**CAIRO, EGYPT**

**2001**

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# ACKNOWLEDGMENT



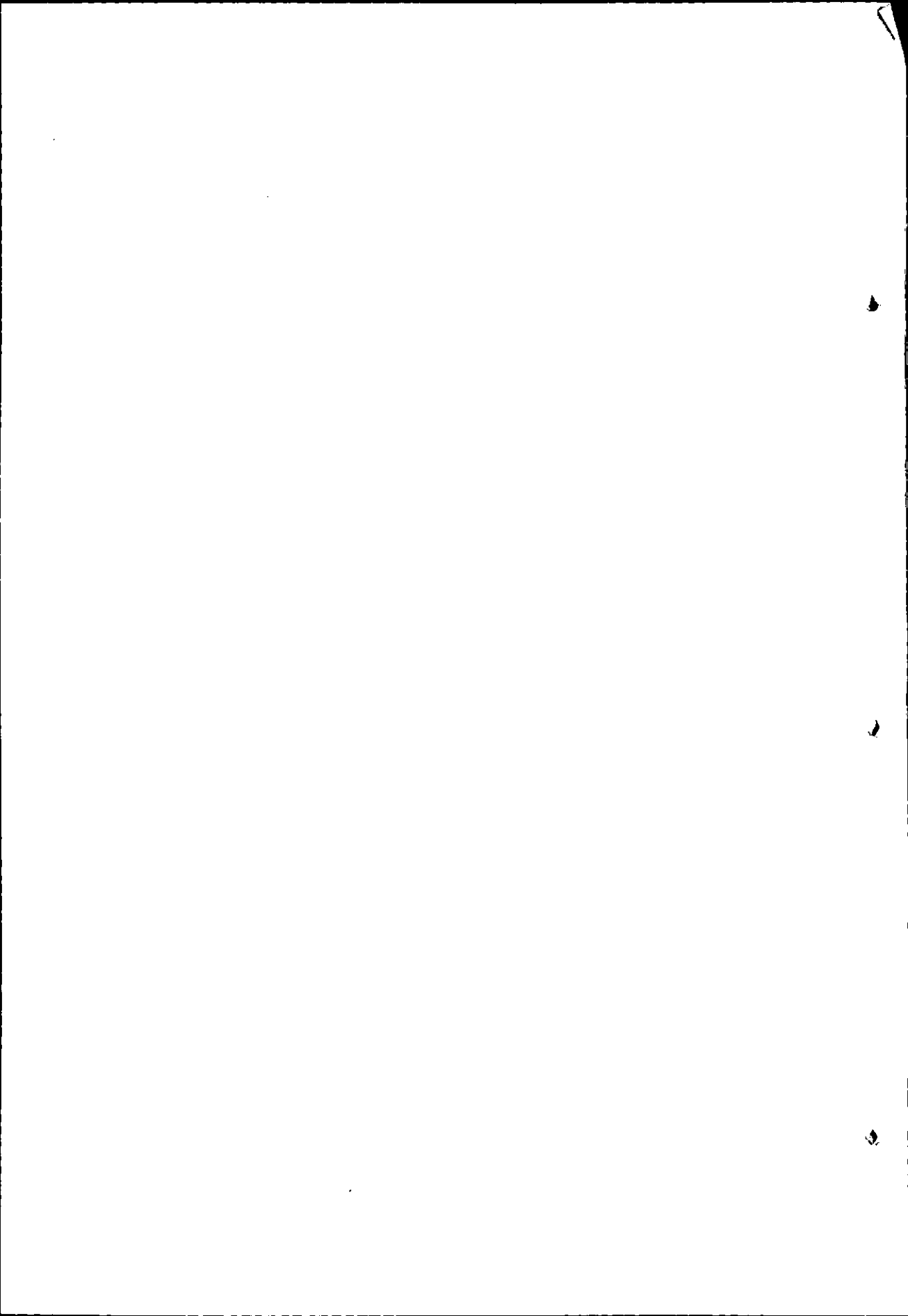


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## ARABIC SUMMARY.

# SUMMARY