



شبكة المعلومات الجامعية

بسم الله الرحمن الرحيم



شبكة المعلومات الجامعية
@ ASUNET



شبكة المعلومات الجامعية التوثيق الالكتروني والميكرو فيلم



شبكة المعلومات الجامعية

جامعة عين شمس

التوثيق الالكتروني والميكروفيلم

قسم

نقسم بالله العظيم أن المادة التي تم توثيقها وتسجيلها
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في درجة حرارة من ١٥-٢٥ مئوية ورطوبة نسبية من ٢٠-٤٠%

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بعض الوثائق الأصلية تالفة

بالرسالة صفحات لم ترد بالاصل

2012

TANTA UNIVERSITY
FACULTY OF ENGINEERING
DEPARTMENT OF ENGINEERING PHYSICS
AND MATHEMATICS

**QUALITATIVE PROPERTIES
OF SOLUTIONS OF NON LINEAR
ORDINARY DIFFERENTIAL EQUATIONS**

**A THESIS
SUBMITTED BY**

*Engineer
Mohamed Abd El - Hamid Khalifa*

TO

*Department Of Engineering Physics
And Mathematics*

FOR

*The Degree " Doctor Of Philosophy " (PH . D .)
In Engineering Mathematics*

SUPERVISED BY

Prof . Dr.

*Mahmoud Ibrahim Hossam El - Din
Prof . Of Engineering Mathematics*

**Head Of Engineering Physics And Mathematics Department
Faculty Of Engineering
Tanta University**

Registered April 1994

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الدراسات العليا

الرسالة للحصول على درجة
دكتوراه الفلسفة في الرياضيات الهندسية

عنوان الرسالة

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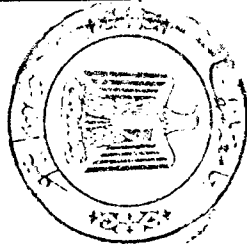
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التوقيع

د. د. محمود ابراهيم حسام الدين «
د. د. محمد يوسف رفاعي «
د. د. إدوارد ميخائيل ابراهيم «

القرار كرسى اللجنة بمنح الطالب / محمد عبد الحميد خليفه
درجة الدكتوراه الفلسفة في الرياضيات الهندسية
مباركة تفاضلية
قسم الفيزياء والرياضيات الهندسية بكلية الهندسة - جامعة طنطا.



« مكتبة »

د. د. وكيل الكلية للدراسات العليا والبحوث

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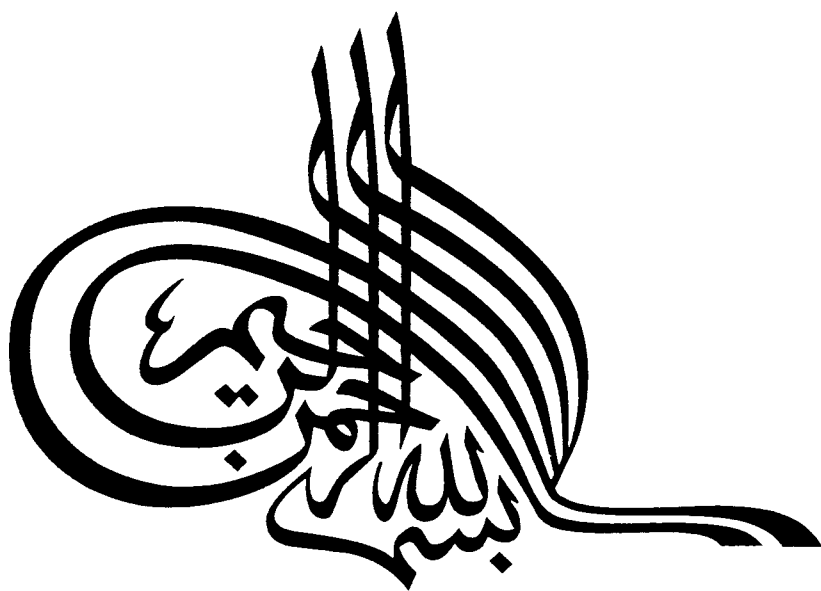
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د. د. عميد الكلية

د. د. جلال عبد الحميد عبد اللاه

د. د. نائب رئيس الجامعة للدراسات العليا والبحوث



علم الانسان ما لم يعلم

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COURSES

Studied successfully by The Author (Oct . 86 - Oct . 87)

During The Preparatory Year For M . Sc . degree

At

Military Technical College , Cairo

- (1) Complex Analysis**
- (2) Numerical Analysis I**
- (3) Probability and Statistics**
- (4) Real Analysis**
- (5) Abstract Algebra**
- (6) Functional Analysis I**
- (7) Analytic Mechanics**
- (8) Linear Programming**
- (9) Topology**
- (10) Partial Differential Equations**
- (11) Ordinary Differential Equations**
- (12) Quantum Mechanics**

COURSES

Studied successfully by The Author (Oct . 1987 - Oct .1988)

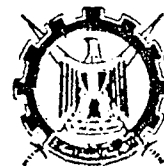
During The 1 st Year for M . Sc . degree

At

Military Technical College , Cairo

- (1) Computer Programming**
- (2) Numerical Analysis II**
- (3) Abstract Linear Algebra**
- (4) Topology and Modern Analysis**
- (5) Calculus of Variations**
- (6) Non - Linear Differential Equations**
- (7) Functional Analysis II**
- (8) Stability Theory**

ARAB REPUBLIC OF EGYPT
MINISTRY OF DEFENCE
MILITARY TECHNICAL COLLEGE
GRADUATE STUDY AFFAIRS



CERTIFICATE

It is hereby certified that :
Engineer : Mohamed Abd El-Hameed Ahmed Khalifa
who was born on 27/8/1949 in El-Gharbiya
has been awarded the degree of

MASTER OF SCIENCE in

ENGINEERING MATHEMATICS

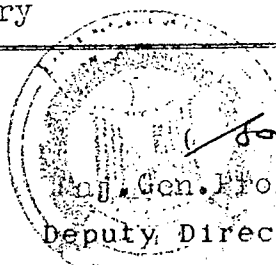
from the MILITARY TECHNICAL COLLEGE on 19/5/1990
after submitting a thesis titled :

"On the Existence and Stability of Periodic Solutions of
Some Ordinary Differential Equations"

The following courses were passed with the indicated grades :

No.	Course Title	Grade
1	Topology & Modern Analysis	Very Good
2	Numerical Analysis	Excellent
3	Abstract Linear Algebra	Excellent
4	Computer Programming	"Good"
5	Calculus of Variations	Very Good
6	Non-linear Differential Equations	Very Good
7	Functional Analysis	Very Good
8	Stability Theory	Very Good

Cairo on : 23/1/1995



Eng. Gen. Prof. Dr. El Saied L. Motwally
Deputy Director for G.S. & Researches

GS Reg. No. 258/1990

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ARABIC SUMMARY	
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SUMMARY