

شبكة المعلومات الجامعية







شبكة المعلومات الجامعية التوثيق الالكتروني والميكروفيلم



شبكة المعلومات الجامعية

## جامعة عين شمس

التوثيق الالكتروني والميكروفيلم

### قسم

نقسم بالله العظيم أن المادة التي تم توثيقها وتسجيلها على هذه الأفلام قد أعدت دون أية تغيرات



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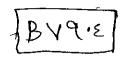
# بعض الوثائـــق الإصليــة تالفــة



# بالرسالة صفحات لم ترد بالإصل



Ain Shams University Faculty of Education Department of Mathematics



## Some Problems of Unsteady Motion of an Electrically Conducting Viscoelastic Fluid

#### A Thesis

Submitted as a Partial Fulfilment for the Requirement of the Degree of Master in Teacher Preparation in Science (Applied Mathematics)

To
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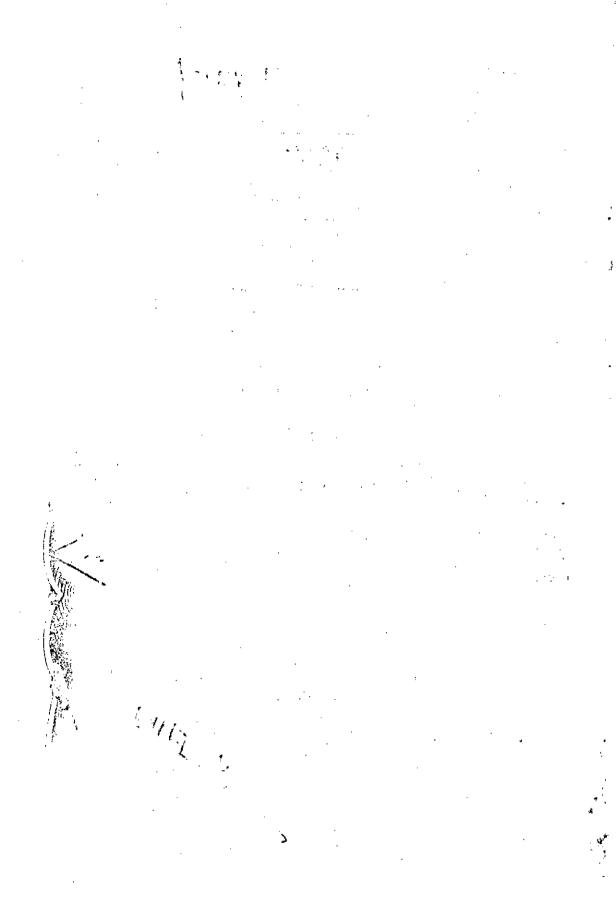
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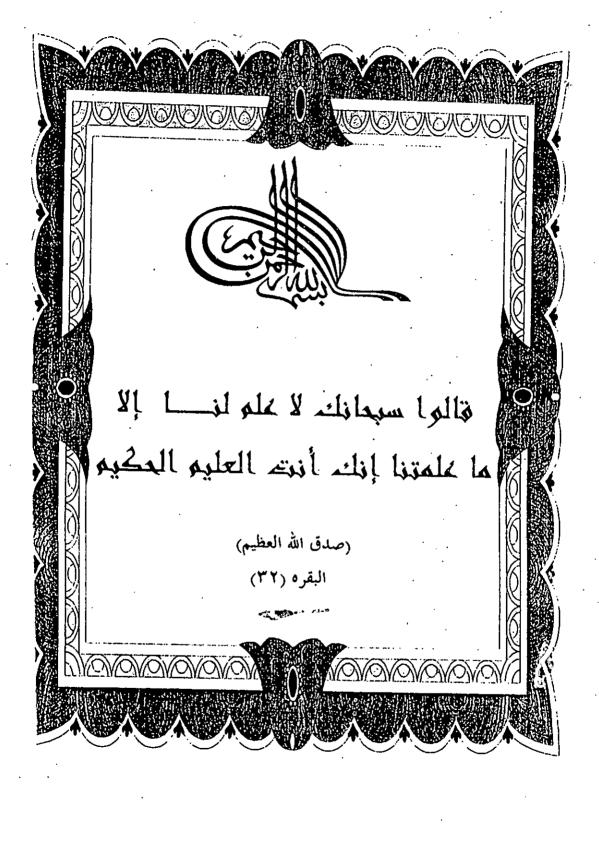
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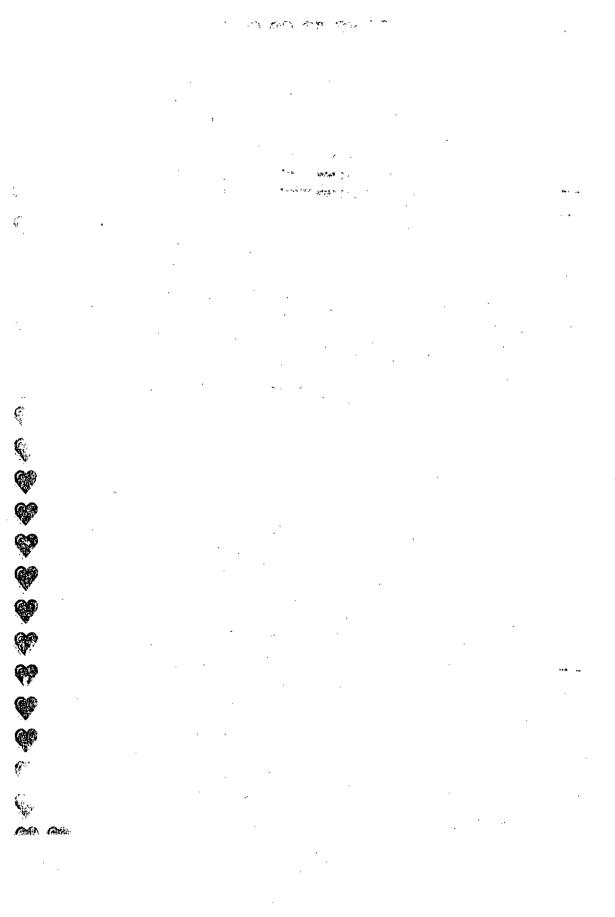
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## To my Family

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