



بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ



شبكة المعلومات الجامعية التوثيق الالكتروني والميكروفيلم



شبكة المعلومات الجامعية

جامعة عين شمس

التوثيق الالكتروني والميكروفيلم

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**OPTIMUM FREQUENCY DESIGN OF CONICAL
SHELL STRUCTURES**

By /

AHMED ISMAIL HASSAN

B.Sc. in Aerospace engineering

**A Thesis Submitted to the
Faculty of Engineering at Cairo University
In Partial Fulfillment of the
Requirement for the degree of**

MASTER OF SCIENCE

in

AEROSPACE ENGINEERING

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