

AIN SHAMS UNIVERSITY FACULTY OF ENGINEERING Electronics and Communication Engineering Department

Time Domain & Frequency Domain Equalizers for Digital Lines

A Thesis

Submitted in partial fulfillment of the requirements of the degree of Master of Science in Electrical Engineering
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شَهِدَ اللّهُ أَنَّهُ لَآ إِلَهَ إِلَّاهُوَ وَالْمَلَتَهِكَةُ وَأُوْلُواْ الْعِلْمِ قَآبِمَا بِٱلْقِسْطِ اللّهَ لَآ إِلَهَ إِلَّاهُوَ ٱلْعَهِيزُ ٱلْحَكِيمُ

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STATEMENT

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No part of this thesis was submitted for a degree or a

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List of Symbols and abbreviations:

δ	A small positive constant.
$\partial \xi / \partial w_k$	The vector of gradient of the mean-square
	error.
a(i)	The desired response.
a_n	The vector of tap-inputs in the feedback
	section.
a _k [n]	Real-valued data sequences operating at a
	sampling rate of F _T .
a_n	System output, training sequence.
b _k [n]	Real-valued data sequences operating at a
	sampling rate of F _T .
c_k	The combination of the feed-forward and
	feed-back tap-weights.
E[.]	The statistical expectation operator.
e_n	The prediction error.
f	SFIR filter.
F _c	Cutoff frequency.
f_{opt}	The optimum shortened filter.
F _T	Transmission frequency.
h_0	The channel impulse response that occur after
	the main sample.
$H_{ch}(f)$	Bandpass frequency response.
$H_{sh}(f)$	The shortened frequency response.
$H_{eq}(f)$	The FEQ equalizer transfer function.
h_e	The estimated channel impulse response.
h_{eq}	The time domain response of equalizer.
$h_{\it eff}$	Effective channel impulse response.
h_{sh}	The shortening impulse response.
h_k	System impulse response.
h_{wall}	Samples outside the window of size N_b from
	the effective channel impulse response.

h_{win}	Samples inside the window of size N_b from
	the effective channel impulse response.
I	The identity matrix.
j_n	The combination of input samples for both
	sections.
L_h	The length of carrier serving area impulse
	response.
N	up-sampled factor
N_b	the desired length of shortened impulse
	response
N_f	Number of taps of SIRF filter.
q_{opt}	The optimum eigenvector corresponding to
	the maximum eigenvalue.
q_{min}	the smallest eigenvector associated with the
	smallest eigenvalue of the matrix C.
$R_{ex}(k)$	The cross-correlation function.
R_{XX}	The correlation matrix.
$\mathbf{u}_{\mathbf{k}}[\mathbf{n}]$	Real sequence.
11	Cyclic prefix.
ν	Cyclic pichix.
$w_k^{(1)}$	The tap-weights of the feed-forward section.
$w_k^{(1)}$ $w_k^{(2)}$	
$w_k^{(1)}$	The tap-weights of the feed-forward section.
$w_k^{(1)}$ $w_k^{(2)}$	The tap-weights of the feed-forward section. The tap-weights of the feed-back section.
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(n)}$	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector.
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(n)}$	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(n)}$ w_k	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector.
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(n)}$ w_k	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector. The vector composed of the impulse response
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(n)}$ w_k W_k	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector. The vector composed of the impulse response samples of the transversal filter.
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(n)}$ w_k W_k W_k	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector. The vector composed of the impulse response samples of the transversal filter. The transpose of <i>W_k</i> .
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(2)}$ $w_k^{(n)}$ w_k W_k W_k	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector. The vector composed of the impulse response samples of the transversal filter. The transpose of W _k . The optimal weight vector.
$w_{k}^{(1)}$ $w_{k}^{(2)}$ $w_{k}^{(2)}$ $w_{k}(n)$ W_{k} W_{k} W_{k}^{T} W_{opt} $x[n]$	 The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector. The vector composed of the impulse response samples of the transversal filter. The transpose of W_k. The optimal weight vector. Composite signal.
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(2)}$ $w_k^{(n)}$ w_k W_k W_k W_k^T W_{opt} $x[n]$ $x_a(t)$	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector. The vector composed of the impulse response samples of the transversal filter. The transpose of W _k . The optimal weight vector. Composite signal. Transmitted analog signal.
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(2)}$ $w_k^{(n)}$ w_k W_k W_k W_k^T W_{opt} $x[n]$ $x_a(t)$	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector. The vector composed of the impulse response samples of the transversal filter. The transpose of W _k . The optimal weight vector. Composite signal. Transmitted analog signal. System input, the vector of tap-inputs in the
$w_k^{(1)}$ $w_k^{(2)}$ $w_k^{(2)}$ $w_k(n)$ W_k W_k W_k^T W_{opt} $x[n]$ $x_a(t)$ x_n	The tap-weights of the feed-forward section. The tap-weights of the feed-back section. The estimate taps weight vector. The set of adaptive filter coefficients, taps weight vector. The vector composed of the impulse response samples of the transversal filter. The transpose of W _k . The optimal weight vector. Composite signal. Transmitted analog signal. System input, the vector of tap-inputs in the feed-forward section.

y(i)	The output produced by N taps transversal filter whose tap inputs (at time i).
y[n]	Received digital signal.
y _a (t)	Received analog signal.
$\alpha_{\mathbf{k}}$	Set of complex sequences.
λ^{n-i}	The forgetting factor.
μ	A small positive constant called the step-size parameter.
ξ	The mean-square error.
Φ [n]	The correlation matrix.

2B1Q	2 binary, 1 quaternary.
4B3T	4 binary, 3 ternary.
ADSL	Asymmetric DSL.
AMI	Alternate mark inversion.
ANSI	American National Standards Institute.
ARMA	Auto-Regressive Moving-Average.
ATM	Asynchronous Transfer Mode.
ATU-C	ADSL Transmission Unit at the Central office.
ATU-R	ADSL Transmission Unit at the Remote.
AWG	American Wire Gauge.
BER	Bit Error Rate.
BRITE	Basic Rate ISDN Transmission Extension.
CAP	Carrier-less Amplitude/Phase modulation.
CDSL	Consumer DSL.
CMA	Constant Modulus Algorithm.
CO	Central Office.
CRC	Cyclic Redundancy Codes.
CSA	Carrier Serving Area.
DFT	Discrete Fourier Transform.
DLC	Digital Loop Carrier.
DMT	Discrete Multi-Tone.
DOCSIS	Data Over Cable System Interface
DOCSIS	Specification.
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DSL	Digital Subscriber Line.
ECH	Echo Cancellation.
FDM	Frequency Division Multiplexing.
FEC	Forward Error Control.
FEQ	Frequency Domain Equalizer.
FFT	Fast Fourier Transform.
FIR	Finite Impulse Response.
FSK	Frequency Shift Keying.
HDSL	High bit rate DSL.
IDSL	ISDN DSL.
IP	Internet Protocol.
ISDN	Integrated Service Digital Network.
ISI	Inter-symbol interference.
LMS	Least-Mean-Square.
LPF	Low-pass filter.
MCM	Multi-Carrier Modulation.
MDF	Main Distributing Frame.
MPEG-1	Moving Pictures Expert Group
MSSNR	The Maximum Shortening SNR.
MSE	Mean Square Error.
MVL	Multiple Virtual Line.
OFDM	Orthogonal Frequency Division Multiplexing.
O. S	Optimal Shortening.