



AIN SHAMS UNIVERSITY  
FACULTY OF ENGINEERING  
CAIRO-EGYPT

# **Microwave Metamaterial**

## **A Thesis**

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## **STATEMENT**

This Thesis is submitted to Ain Shams University in partial fulfillment of the degree of Master of Science in Electrical Engineering.

The work included in this thesis was carried out by the author in the department of electronics and communication engineering, Ain Shams University.

No part of this Thesis has been submitted for a degree or a qualification at any other university or institute.

Name : Marwah Ahmed Mohamed Shafee

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*To My Parents*

*I present to you this thesis to express my deep  
gratitude and love*

*Thanks*

---

# Microwave Metamaterial

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## ABSTRACT

A new category of microwave metamaterial structures named as *high-impedance wire* (HIW); is studied in this thesis. The characteristics of HIWs allow the engineering of dispersion relation of transmission lines. High impedance wires offer two main benefits; size reduction and multiple operating bands. New implementation for HIWs, Signal-HIW, was proposed and it was used in miniaturizing some microwave devices.

Four applications based on the Signal-HIW are proposed. First application is combining two HIWs in one structure to form a HIW-TL. HIW-TL has interesting dispersion characteristics, it has three independent bands of operation. Second application is compact HIW rat-race coupler. The new coupler is made by replacing the rat-race ring with a Signal-HIW. The proposed coupler size is reduced by 44.7% from the conventional implementation. Third application is a new implementation for compact dual-mode filter. The filter circuit model is also derived. Finally, the design of a patch antenna using Signal-HIW was studied. The design flow for the antenna was developed. The new patch antenna occupies only 45.6% of conventional patch area.

All the proposed devices were fabricated and measured. The measurements results were compared with simulations. Very good agreements were achieved.

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