



Ain Shams University
Faculty of Science
Department of Mathematics

On the Generalization of Some Exponentiated Distributions using Beta Distribution

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By
Noha Mohamed-Kamal Nada
Master degree (Mathematical Statistics)
Ain Shams University, 2009

Under Supervision of

Dr. N.L. Bassily,
Emeritus Ass. Prof. of
Mathematical Statistics,
Mathematics Department,
Faculty of Science,
Ain Shams University.

Dr. M. M. Nassar,
Ass. Prof. of Mathematical Statistics,
Mathematics Department,
Faculty of Science,
Ain Shams University.

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