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# شبكة المعلومات الجامعية

## التوثيق الالكتروني والميكرو فيلم

# جامعة عين شمس

التوثيق الالكتروني والميكرو فيلم

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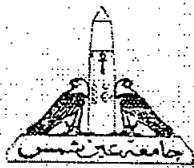
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بالرسالة صفحات  
لم ترد بالأصل



Ain Shams University  
Faculty of Science  
Mathematics Department

# ON TEMPORAL LOGIC

A THESIS  
SUBMITTED FOR THE DEGREE OF Ph.D. IN SCIENCE  
(Computer Science)

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## **Abstract**

The aim of the proposed study is to arrive a new concept in Temporal Logic of Actions (TLA) which is one of the important branches in artificial intelligence. It is designed for the specification and verification of reactive systems in terms of their actions. The research in that way is a new contribution; which will help in investigating the aims and properties of programming in its general form.





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