**Physics Department Faculty of Science Ain Shams University** 



# Study on Collective Behavior of Plasma Waves in Degenerate Plasma

A Thesis submitted in partial fulfillment of the requirements for the degree of Master of Science in Physics

### By

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2016

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# **Acknowledgements**

All Praises to Almighty Allah, the most merciful and the Creator of the whole universe, who enabled me to complete this research work successfully.

I would like to express my sincere and hearty appreciation to my supervisors Prof. Dr. Salah Yaseen Elbakry and Prof. Dr. Bahaa Eldin Fouad Mohamed for their constant encouragement, constructive guidance and helpful suggestions during this research work. Prof. Dr. Salah Yaseen Elbakry always behaves as a father before as a supervisor. And Prof. Dr. Bahaa Eldin Fouad Mohamed gives me a lot of self-confidence to research more and more. He always follows the work seriously and determined the next step, then helps me to achieve it. He taught me the procedure to make great scientific research from A to Z. I deeply appreciate his energy, and ability to see and formulate new and exciting physical problems.

Also, a great thanks to my supervisor in my research work, Assoc. Prof. Dr. Esraa Ali Elkhateeb for many valuable discussions, initial guidance, encouragements and for reviewing the whole thesis. She also give me from her knowledge and experience.

Besides my supervisors, it is a pleasure to thank the first one who encouraged me to enter the plasma world and make research in this field, as it is very interesting and there will be a great development in it in the future, Prof. Dr. Mostafa Shalaby, asking ALLAH to be in Paradise. He was also as spiritual father for me, and I was always taken his opinion in my going steps.

Also, a lot of thanks to the staff of the Theoretical Plasma Physics Department at Nuclear Research Center (N.R.C.), especially Prof. Dr. Bahaa-Eldin Fouad Mohamed, and the staff of the Physics Department at the Faculty of Science, Ain-Shams University, especially the head of the Department, Prof. Dr. Salah Yaseen Elbakry, and the coworkers Dr. Lamiaa Samir, Nermin Elbasha, Manar Ahmed, Reem Mohamed and Mohamed Adel for providing support and facilities when needed.

Finally, my deepest gratitude goes to all of my family, especially to my loving parents, grandparents, sisters and brothers who always prayed for my success and supported me. And great thanks to my little family, my caring husband Ayman Osama and our little angel Belal, who suffered with me a lot and sustained my shortening with them, but always stand beside me with their best wishes to complete my work and success.

# Contents

| Acknowledgements i                     |
|--|
| List of Figuresvi                      |
| Abstractix                             |
| Key wordsx                             |
| Chapter (1)1                           |
| Introduction1                          |
| 1.1. Classical and Quantum Plasmas2    |
| 1.2. Conditions of Plasma6             |
| 1.2.1. Debye Shielding6                |
| 1.2.2. Density in Debye Sphere8        |
| 1.2.3. Criteria of Plasma9             |
| 1.3. Characterization of Plasma9       |
| 1.3.1. Plasma Frequency9               |
| 1.3.2. Temperature of Plasma11         |
| 1.3.3. Energy Coupling Parameter13     |
| 1.4. Appearance of Plasmas in Nature15 |
| 1.5. Applications of Plasma Physics17  |
| 1.6. Waves in Plasma                   |

| 1.6.1.     | Surface Waves                      | 28 |
|------------|------------------------------------|----|
| 1.7. Quar  | ntum Plasma                        | 32 |
| 1.7.1.     | Quantum Plasma Description         | 33 |
| 1.7.2.     | Quantum Effects                    | 34 |
| 1.7.3.     | Applications of Quantum Plasma     | 37 |
| 1.8. Semi  | conductor Plasmas                  | 38 |
| 1.9. Previ | ous Work                           | 41 |
| 1.10. Aim  | of the Work:                       | 42 |
| Chapter (2 | 2)                                 | 44 |
| Models fo  | r Studying Plasmas                 | 44 |
| 2.1. Class | ical Models                        | 44 |
| 2.1.1.     | Kinetic Model                      | 45 |
| 2.1.2.     | Vlasov Model                       | 48 |
| 2.1.3.     | Hydrodynamic Model                 | 49 |
| 2.2. Quar  | ntum Models                        | 50 |
| 2.2.1.     | Schrödinger-Poisson Model          | 51 |
| 2.2.2.     | Wigner-Poisson Model               | 53 |
| 2.2.3.     | Quantum Hydrodynamic Model         | 56 |
| 2.2.4.     | Quantum Magneto-hydrodynamic Model | 59 |
| Chapter (3 | 3)                                 | 62 |

| Theoretical Treatment of Surface Waves in Degenera Plasmas                 | te |
|--|----|
| 3.1. Surface Waves Excitation in Magnetized Sp Quantum Plasmas             |    |
| 3.1.1. Model of Equations63  |    |
| 3.1.2. Dispersion Relations68  |    |
| 3.1.3. Numerical Solution70  |    |
| 3.2. Electrostatic Surface Modes in Magnetized Quantu Electron-Hole Plasma |    |
| 3.2.1. Model of Equations77  |    |
| 3.2.2. Dispersion Relations82  |    |
| 3.2.3. Numerical Solution84  |    |
| Chapter (4)90  |    |
| Summary and Conclusion87   |    |
| Summary  | 37 |
| Conclusion   | 39 |
| References90   |    |

# List of Figures

| Fig. (1.1)  | Debye Shielding.  | 6  |
|-------------|---|----|
| Fig. (1.2)  | Mechanism of the plasma oscillations.   | 10 |
| Fig. (1.3)  | A maxwellian distribution of velocity.  | 11 |
| Fig. (1.4)  | Spatial variation of the electric field of two waves with a frequency difference.                                 | 19 |
| Fig. (1.5)  | Dispersion relation for electron plasma waves.  | 20 |
| Fig. (1.6)  | Geometry of an electrostatic ion cyclotron wave propagating nearly at right angles to $\vec{B}_0$ .               | 22 |
| Fig. (1.7)  | Geometry of Electromagnetic waves propagating at right angles to $\vec{B}_0$ .                                    | 23 |
| Fig.(1.8)   | The E-vector of an extraordinary wave is elliptically polarized.  | 23 |
| Fig. (1.9)  | Geometry of right- and left-handed circularly polarized waves propagating along $\vec{B}_0$ .                     | 24 |
| Fig.(1.10)  | Geometry of Alfvén wave propagating along $ec{B}_o$ .   | 25 |
| Fig. (1.11) | Relation among the oscillating quantities in an Alfvén wave and the exaggerated distortion of the lines of force. | 25 |

| Fig. (1.12) | Geometry of a magnetosonic wave propagating at right angles to $\vec{B}_o$ .   | 26 |
|-------------|--|----|
| Fig. (1.13) | Schematic band structure with energy gap $E_{g}^{}$ .  | 38 |
| Fig. (3.1)  | Dispersion relations of electromagnetic TM surface modes in quantum unmagnetized plasma ( $\overline{\omega} = 0$ ) for different quantum effect ratios ( $H = 0,1,2,3,4$ ).   | 70 |
| Fig. (3.2)  | Different solutions of dispersion relation (3.21) for different electromagnetic surface modes in quantum magnetized plasma.  | 71 |
| Fig. (3.3)  | Two different solutions of dispersion relation (3.21) for electromagnetic TM surface modes in quantum magnetized plasma ( $\bar{\omega}$ = 0.1) for different quantum ratios ( $H$ = 1, 2, 3, 4).  | 72 |
| Fig. (3.4)  | Dispersion relations of electromagnetic TM surface modes in quantum magnetized plasma $(\bar{\omega} = 0.1, 0.2, 0.3)$ with quantum ratio $(H = 1)$ .  | 73 |
| Fig. (3.5)  | Solution of dispersion relation of electromagnetic surface modes in quantum magnetized plasma with and without spin effect ( $\bar{\omega}$ = 0.1 and $H$ =1).   | 74 |
| Fig. (3.6)  | Dispersion relations of electrostatic surface modes for density ratio ( $\delta$ = 0.1) in classical unmagnetized electron-hole plasma ( $\omega_{ch}$ = 0), ( $H$ = 0). (a) is a solution of Eq. (3.39), (b) and (c) are solutions of Eq. (3.43). | 83 |
| Fig. (3.7)  | Dispersion relation of electrostatic surface modes for different density ratios  | 84 |

|             | ( $\delta$ = 0.1,0.3,0.5,0.9) in unmagnetized quantum plasma ( $\omega_{ch}$ = 0 , $H$ = 0.1).   |    |
|-------------|--|----|
| Fig. (3.8)  | Two dispersion relations of the surface modes for different magnetic fields ( $\omega_{ch}=0.1,0.3,0.5,0.7$ ) in classical plasma ( $H=0$ ) with electron-hole density ratio ( $\delta=0.1$ ). | 85 |
| Fig. (3.9)  | Dispersion relation of the electrostatic surface modes for different quantum ratios $(H=0.1,0.3,0.5,0.7,0.9)$ in unmagnetized quantum plasma with electron-hole density ratio $(\delta=0.3)$ . | 85 |
| Fig. (3.10) | Dispersion relation of electrostatic surface modes with variation of quantum effect in magnetized electron-hole plasma with $\omega_{ch}=0.1$ and $\delta=0.1$ .                               | 86 |

# **Abstract**

The present study concentrates on investigation of the collective behavior of surface plasma waves in degenerate plasma. It has been studied the effect of the different quantum effects (Fermi pressue, Bohm potential, and spin effect) on the excitation of the surface waves in quantum plasma under the influence of an external magnetic field. The effect of the previous quantum effects on the propagation of the electrostatic surface waves in electron-hole plasma has also been investigated.

The impact of the radical spin of electrons on the excitation of transverse electromagnetic surface waves in a magnetized quantum plasma is inspected. The quantum corrections arises from the Bohm potential and the magnetization energy of electrons due to their spins are taken into considration by employing a fluid formalism. Also, the excitation of electrostatic surface waves on a semi-bounded quantum plasma-vacuum interface parallel to an applied magnetic field with electron-hole degeneracy is investigated. The wave equations of the electrostatic potential and both of the perturbed electron and hole plasma densities have been solved analytically. The general dispersion relation of the surface modes is obtained.

It is found that the inclusion of the quantum effects give rise to the excitation of possible surface modes. The phase and group velocities of the surface plasma waves are increased due to the inclusion of the different quantum effects in both electromagnetic and electrostatic cases. Also, it has been found that the density ratio of hole-electron plasma plays an essential role on the

dispersion of the modes along the wavenumber in addition to the effect of the quantum effects and the magnetic field.

The previous results can be used to improve the efficiency of data transfer in the computer chips which based on the performance of the semiconductors. Data can be transferred on the surface by the surface waves without suffering diffraction. Also, the velocity of data transfer process can be increased by increasing the hole-electron density ratio.

# Key words

Quantum plasma, quantum effects, Bohm potential, surface plasma wave (SPW), quantum magneto-hydrodynamic model (QMHD), spin quantum plasma, electron-hole plasma.

# Chapter (1)

# Introduction

The word plasma is a Greek word means moldable substance or jelly. The first one who used the term plasma to describe an ionized gas was Irving Langmuir in 1927. He was awaken to the way blood plasma carries white and red pellets by the way an electrified fluid carries ions and electrons. Langmuir, with Lewi Tonks in the main time, was researching the chemistry and physics of tungsten-filament light-bulbs, trying to find a way to extend its lifetime. He notice that certain regions of a plasma discharge tube displays periodic variations of the density of the electron, which we term Langmuir waves nowadays. This was the origin of the Plasma Physics. Nowadays, Langmuir's research forming the theoretical basis of most techniques of plasma processing for the fabrication integrated circuits (Fitzpatrick 2014).

Plasma is sometimes referred to as "the fourth state of matter". It is a gas that the atoms in it have been broken up into free negative electrons and positive ions, atoms that have lost electrons and become positively charged.

Of course, not any ionized gas can be referred to as a plasma; in any gas there is always some small degree of ionization. We can define the plasma as "a quasi-neutral gas of charged and neutral particles which exhibits collective behavior". As the Quasi-neutrality means that if the dimension

L of the system is much larger than the Debye length  $\lambda_D$ , then whenever external potential is introduced into the system or local concentrations of charge arise, these are shielded out in a distance that is short compared with the dimension of the system L, leaving the bulk of the ionized gas free of large fields or electric potentials. And Collective behavior means that as the charged particles move, they can produce local concentrations of negative or positive charge, which rise the electric fields. Also, movement of charges produces currents, so magnetic fields. These fields, far away, effect on the movement of other charged particles (Chen and Von Goeler 2008).

# 1.1. Classical and Quantum Plasmas

Fluids are intense that we can ignore the movement of individual molecules. Furthermore, only single particle tracks are considerable in very low-density devices; collective effects becomes unimportant. Plasma, on the other hand, behaves sometimes like a collection of individual particles and in another times as fluids. Generally, a plasma is understood as a many-body system consists of a large number of charged particles, while its behavior is controlled by collective effects that are arranged by the electromagnetic force.

The temperature is an essential parameter of plasma. Our early universe was formed a 100% of plasma. According to Big Bang theory, the temperature was high enough that no molecules or atoms could have existed, but only the fully