



# EVALUATION OF CARDIAC GLOBAL FUNCTION USING REDUCED NUMBER OF MR IMAGES

By

Hossam Ahmed Mohammad El-Rewaidy

A Thesis Submitted to the
Faculty of Engineering - Cairo University
in Partial Fulfillment of the
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Under the Supervision of

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FACULTY OF ENGINEERING, CAIRO UNIVERSITY GIZA, EGYPT 2016

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**Title of Thesis:** 

Evaluation of the Cardiac Global Function using Reduced Number of MR Images

#### **Key Words:**

Cardiac Global Function, Volume Calculation, Surface Reconstruction, Right Ventricle Segmentation, Active Shape Model, Geometric Models, Cardiac Modeling.

#### **Summary:**

Evaluating the heart global function from magnetic resonance images is based on estimating a number of functional parameters such as the left ventricular (LV) and right ventricular (RV) volumes, LV and RV masses, ejection fraction, and stroke volume. Estimating these parameters requires: First, accurate segmentation of the main cardiac champers, LV and RV. LV segmentation can be done by many techniques with a plausible performance; However, RV segmentation is still a challenging problem due to the complex shape of the RV, presence trabecular muscles and low tissue-to-blood contrast. Second, accurate calculation of the volumes enclosed by the inner and outer surfaces of the LV and RV chambers. Currently, the volume calculation is achieved through acquisition and segmentation of a large number of short-axis (SAX) crosssections of the LV and RV, which is time-consuming, expensive and causing patient inconvenience. Unfortunately, reducing the number of the acquired cross-sections results in undersampling the LV surfaces and hence increases the errors of calculating the volume. In this thesis, we propose two packages of novel methods in both RV segmentation and volume calculation from small number of MR slices. In RV segmentation, an Active Shape/Appearance Model (ASM) based system is introduced for accurately segmenting the RV from MR short axial (SAX) images. The RV shape variations are independently modeled using two separate (dual) ASM models in the Bookstein domain. In order to better segment the low contrast regions at the apex, the method is extended for multiple-2D images where the variations of all cardiac levels are incorporated in a single model. For the volume calculation, new method based on fusing the long axial (LAX) and SAX views of the heart is presented. In this method, the LAX contour is used to swipe the SAX contours to fill in the missed LV surface between the SAX slices. Furthermore, novel geometrical models that combine information from SAX and (LAX) views are invented. The results from 25 datasets and 5 CT-based phantom showed that our methods outperform most of the used methods in the literature.

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### Acknowledgment

Firstly, I would like to express my sincere gratitude to my advisor *Dr. Ahmed Fahmy* for the continuous support of my Master's study and related research, for his patience, motivation, and immense knowledge. His guidance helped me in all the time of research and writing of this thesis. I could not have imagined having a better advisor and mentor for my Master's study.

Besides my advisor, I would like to thank *Dr. Ayman Khalifa*, *Dr. Inas Yassine* and *Dr. El-Sayed Ibrahim*, for their insightful comments and encouragement, but also for the hard question which incented me to widen my research from various perspectives.

I thank also all my fellows and friends at Cairo and Nile universities, and Diagnosoft Inc. for the stimulating discussions and support.

Last but not the least, I would like to thank my family: my parents and, my brothers and sisters for supporting me spiritually throughout writing this thesis and my life in general. I would like also to express my special heartfelt gratitude to my mother for her sincere praying for me all the time.

## **Dedication**

To those persons who inspired me and changed my life for better.

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1ast 10w, the agreement detween monny and the ground truth at 4 and 0 snees

#### **Nomenclature**

2-CH Two Chambers

4-CH Four Chambers

AP Anterior-Posterior direction

ASM Active Shape Model

CO Cardiac Output

DCM Dilated Cardiomyopathy

EDV End-Diastolic Volume

EF Ejection Fraction

ESV End-Systolic Volume

FR Free Wall

HR Heart Rate

IHD Ischemic Heart Diseases

LAX Long Axial

LR Left-Right Direction

LV Left Ventricle

LVM Left Ventricular Mass

MAD Mean Absolute Value

MP Mid-Papillary Muscles

MRI Magnetic Resonance Imaging

mSimp Modified Simpson's Method

MV Mitral Valve

PCA Principal Component Analysis

PDM Point Distribution Model

PVE Partial Volume Effect

RCM Restrictive Cardiomyopathy