



AIN SHAMS UNIVERSITY
FACULTY OF ENGINEERING
STRUCTURAL ENGINEERING DEPARTMENT

BEHAVIOR OF LIGHTWEIGHT CONCRETE UNDER UNIAXIAL ECCENTRIC COMPRESSIVE STRESSES

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The candidate confirms that the work submitted is his own and that appropriate credit has been given where reference has been made to the work of others

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