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Electronic Structure and Magnetic Properties of Rare Earth Transition Metal (RT_5 Compounds)

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Dedicated To

My Husband & Sons

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