



شبكة المعلومات الجامعية

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ





شبكة المعلومات الجامعية



شبكة المعلومات الجامعية

التوثيق الالكتروني والميكرو فيلم

جامعة عين شمس

التوثيق الالكتروني والميكرو فيلم

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بالرسالة صفحات
لم ترد بالأصل

EXACT TESTS IN RANDOM AND MIXED LINEAR MODELS

A THESIS

**Submitted to Mathematics Department,
Faculty of Science, Tanta University,
In Partial Fulfillment of the
Requirements for the Degree
of Master of Science**

IN

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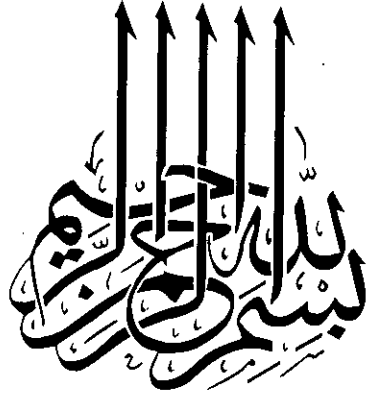
BY

**Mohamed Mohamed Ezzat
Abd El-Monsef**

**Department of Mathematics
Faculty of Science
Tanta University**

2001

B. 7110



وَقُلْ رَبِّ زِدْنِي عِلْمًا



B 7110

SUPERVISORS

1. Prof. Dr. Entesar Mohamed El-Kholy

*Professor of Mathematics, Head of Mathematics
Department, Faculty of Science, Tanta University.*

2. Prof. Dr. EL-Houssainy Abd EL-Bar Rady

*Professor of Statistics, Institute of Statistical Studies
and Research, Cairo University.*

3. Dr. Hala Aly Ibrahim Fergany

*Lecturer of Mathematical Statistics, Department of
Mathematics, Faculty of Science, Tanta University.*

Head of Mathematics Department

E. EL-Kholy

Prof. Dr. E. M. El-Kholy

CURRICULUM VITÆ

Name : Mohamed Mohamed Ezzat Abd El-Monsef.
Date of Birth : 1/11/1976.
Locality : Tanta – Gharbia.
Nationality : Egyptian.
Qualifications : B. Sc. in Mathematical Statistics (1998),
Excellent Grade (Hons).
Present State : Demonstrator of Mathematical Statistics,
Mathematics Department, Tanta University.
Social Status : Single.
Permanent adders : 1 Othman Mohamed St., Tanta.
E-mail : mme@dr.com.

Head of Mathematics Department

E. EL-Kholy

Prof. Dr. E. M. El-Kholy

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ

" رب أوزعني أن أشكر نعمتك التي أنعمت عليّ وعلى والدي وأن أعمل صالحاً ترضاه وأصلح لي في ذريتي إني تبت إليك وإني من المسلمين "

صداق الله العظيم

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NOTE

The present Thesis is submitted to Tanta University in partial fulfillment of the requirements of the degree of Master of Science in Mathematical Statistics.

Beside the research work introduced in this Thesis, the candidate has attended four graduate courses within two years including

1. *Probability Theory*
2. *Stochastic Process*
3. *Queuing Theory*
4. *Distribution Theory*

The applicant *Mohamed Mohamed Ezzat Abd El-Monsef* has successfully passed the final examination (1999 – 2000) of these courses.

Head of Mathematics Department

E. EL-Kholy
Prof. Dr. E. M. El-Kholy

PREFACE

Experiments are performed by people in nearly all aspects of life. The basic reason for running an experiment is to find out something that is not known. By their very nature, experiments are designed to draw inferences about an entire population based on few observations.

If experiments were perfectly repeatable and the important factors were perfectly separable, it would be easy to analyze and interpret the results. However, experiments are often run so that the effect of one factor may unknowingly be confounded with the effect of a factor not considered in the experiment. Even with the best of the experimental control, results vary from trial to trial. These reasons, and many others, add to the difficulty in analyzing the data derived from an experiment.

The role of statistics in experimental design is to separate the observed differences into those caused by various factors and those due to random fluctuation. The classical method used to separate these differences is analysis of variance, or ANOVA. In general, the method consists of looking at the total variation in the data, breaking it into its various components, and running statistical tests in an attempt to find out which components influence the experiment.

The analysis of balanced data, *data with equal numbers of observations in the subclasses*, is fairly straightforward since the ANOVA decomposition of the total sum of squares is unique and the different sums of squares in such decomposition provide tests for various hypotheses of interest, even in some cases we can't perform exact tests for some effects. In contrast to balanced data, the analysis of unbalanced data, *data with unequal numbers*

The Thesis consists of **five chapters**. In the introductory *Chapter I* we recall most of the definitions and preliminaries to be used throughout this Thesis. Moreover, we introduce some propositions and results concerning fundamental concepts of this work.

The aim of *Chapter II* covers exact tests for the unbalanced one-way, random two-way with interaction, mixed two-way models. Also, random two-stage nested model and the general random nested models were covered.

Chapter III presents the *Error Contrasts Technique*. Its properties and its uses for constructing exact tests will be introduced.

The purpose of *Chapter IV* is to introduce exact tests for some random and mixed balanced models using the proposed technique. We derived also an exact test for the main effects in the three-way random model, which can't be made using ANOVA procedure.

Chapter V deals with the case of unbalanced random and mixed models. An exact test for testing the hypothesis in *Khuri's* (1990) model, which he failed to find an exact test for it, will be made using the *Error Contrasts Technique*.

The last chapter followed by references. Both *Chapters II & III* comprised a section of some useful remarks.

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