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Transmission Techniques for Multi-User MIMO Communications

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by

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*To **Sarah**, my daughter and friend.*

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