



Cairo University

# DESIGN OF NEW IMAGE ENCRYPTION SYSTEMS USING CHAOS THEORY AND FRACTALS

By

Sherif Hamdy AbdElHaleem Mohamed

A Thesis Submitted to the  
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in Partial Fulfillment of the  
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**Title of Thesis:**

**Design of New Image Encryption Systems Using Chaos Theory and Fractals**

**Key Words:**

Cryptography; Cryptanalysis; Image Encryption; Information Security; Fractional-Order; Fractals; Generalized Feistel Networks; Linear Feedback Shift Register; S-Boxes; Keystream Generator; Chess; Horse Movement; Permutation Matrix; Chaotic equations; Chaotic Maps.

**Summary:**

This thesis introduced seven new encryption designs based on different methodologies such as: chaotic differential equations of integer and fractional-orders, nonlinear generalized chaotic maps, fractals with their fine details, mixing the generalized Fiestel network with the Linear Feedback Shift Register (LFSR) and, also, a new encryption system based on the chess-based horse-move to generate the permutation matrix. Many standard images were discussed and evaluated using the international measures such as NIST. Seven international papers were published (2 journal papers with IF + five international conferences).

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## **Dedication**

I dedicate this work to my family. Their support and encouragement have been very inspiring to me. Many thanks are due to my mother who pushed me forward to continue this thesis. Many thanks are also due to my father, who is my role model in life.

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# Table of Contents

<b>ACKNOWLEDGMENTS.....</b>	<b>I</b>
<b>DEDICATION .....</b>	<b>II</b>
<b>TABLE OF CONTENTS .....</b>	<b>III</b>
<b>LIST OF TABLES.....</b>	<b>VI</b>
<b>LIST OF FIGURES.....</b>	<b>VIII</b>
<b>NOMENCLATURE .....</b>	<b>XI</b>
<b>ABSTRACT .....</b>	<b>XII</b>
<b>CHAPTER 1 : INTRODUCTION .....</b>	<b>1</b>
1.1.    ORGANIZATION OF THE THESIS.....	3
<b>CHAPTER 2 : BACKGROUND AND RELATED LITERATURE .....</b>	<b>4</b>
2.1.    HISTORY OF CRYPTOGRAPHY .....	4
2.2.    OVERVIEW OF CRYPTOGRAPHY .....	6
2.2.1.    Symmetric and asymmetric key cryptography .....	7
2.2.2.    Stream and block ciphers.....	9
2.2.3.    Block ciphers modes of operation .....	9
2.3.    IMAGE ENCRYPTION .....	12
2.3.1.    Digital image .....	12
2.3.2.    Encryption evaluation techniques.....	18
2.3.2.1.    Statistical tests .....	18
2.3.2.2.    Sensitivity tests .....	24
2.4.    ENCRYPTION SYSTEMS.....	27
2.4.1.    System key.....	27
2.4.2.    Encryption blocks .....	29
2.4.3.    Pseudo random number generator (PRNG).....	31
2.4.3.1.    Discrete maps .....	34
2.4.3.2.    Continuous systems .....	36
2.5.    RELATED LITERATURE .....	38
<b>CHAPTER 3 : NEW STREAM CIPHERS BASED ON NON-CHAOTIC GENERATORS .....</b>	<b>42</b>
3.1.    IMAGE ENCRYPTION BASED ON LFSR AND FEISTEL NETWORKS .....	43
3.1.1.    The simplified system.....	43
3.1.1.1.    LFSR .....	43
3.1.1.2.    Simulation Results.....	44
3.1.2.    The proposed encryption system .....	45
3.1.2.1.    Generalized Feistel network .....	46
3.1.2.2.    Substitution box (S-box).....	46
3.1.2.3.    System key .....	47
3.1.3.    Analysis results.....	48
3.2.    A FRACTAL-BASED IMAGE ENCRYPTION SYSTEM .....	51

3.2.1.	Fractal images .....	51
3.2.2.	A simplified encryption system .....	54
3.2.3.	The proposed encryption system .....	56
3.2.3.1.	System block diagrams .....	56
3.2.3.2.	System key .....	58
3.2.4.	Multi-fractal encryption.....	60
3.2.4.1.	Sensitivity analysis .....	63
3.2.4.2.	Comparison with previous work.....	66
3.3.	A PSEUDO RANDOM KEY GENERATOR .....	67
3.3.1.	The proposed PRKG.....	67
3.3.1.1.	SPN .....	67
3.3.1.2.	Fractal images.....	68
3.3.1.3.	The proposed PRKG based on fractals .....	69
3.3.2.	PRKG results .....	70
3.3.3.	Image encryption using the proposed PRKG.....	73
<b>CHAPTER 4 : NEW STREAM CIPHERS BASED ON CHAOTIC GENERATORS .....</b>		<b>76</b>
4.1.	IMAGE ENCRYPTION BASED ON GENERALIZED DISCRETE MAPS .....	77
4.1.1.	Generalized logistic, tent and sine maps.....	78
4.1.1.1.	Logistic map .....	78
4.1.1.2.	Tent map.....	79
4.1.1.3.	Sine map.....	79
4.1.2.	System block diagram.....	80
4.1.3.	Encryption results .....	81
4.1.4.	Encryption based on the generalized sine map .....	85
4.1.4.1.	System key .....	86
4.1.4.2.	Encryption results.....	87
4.1.4.3.	Sensitivity analysis .....	89
4.1.4.4.	Additional results and comparisons.....	90
4.2.	IMAGE ENCRYPTION IN THE FRACTIONAL-ORDER DOMAIN .....	92
4.2.1.	Fractional-order chaotic systems .....	92
4.2.1.1.	Chaotic maps .....	92
4.2.1.2.	Fractional-order derivatives.....	93
4.2.1.3.	Fractional-order lorenz map .....	94
4.2.1.4.	Strange attractors .....	94
4.2.2.	The encryption algorithm.....	94
4.2.3.	Analysis results.....	95
4.2.3.1.	System parameters and initial values.....	95
4.2.3.2.	Histogram analysis .....	96
4.2.3.3.	Pixel correlation analysis.....	96
4.2.3.4.	Sensitivity analysis .....	99
4.2.3.5.	Differential attacks .....	99
<b>CHAPTER 5 : NEW SYSTEMS FOR BLOCK-BASED ENCRYPTION .....</b>		<b>100</b>
5.1.	CHESS-BASED IMAGE ENCRYPTION.....	101
5.1.1.	The proposed chess-based chaotic cipher .....	101
5.1.1.1.	Substitution process .....	101
5.1.1.2.	Chess-based permutation process .....	103
5.1.1.3.	System key .....	104
5.1.2.	Evaluation of the encryption system.....	105
5.1.2.1.	Substitution and permutation processes analysis results.....	106

5.1.2.2.	Proposed block cipher analysis results .....	106
5.1.2.3.	Sensitivity analysis .....	108
5.2.	COMPARISON OF DIFFERENT PERMUTATION TECHNIQUES AND THEIR EFFECT ON IMAGE ENCRYPTION.....	110
5.2.1.	Permutation techniques.....	110
5.2.1.1.	Matrix generation using discrete chaos.....	111
5.2.1.2.	Matrix generation using permutation vectors .....	111
5.2.1.3.	Arnold's cat map .....	112
5.2.1.4.	Matrix generation using continuous chaos .....	112
5.2.1.5.	Matrix generation using chess-based horse move.....	113
5.2.2.	Permutation comparisons.....	115
5.2.2.1.	Permutation matrix analysis .....	115
5.2.2.2.	Algorithm results and analysis.....	117
5.2.3.	Image encryption using the five techniques.....	121
5.2.3.1.	System key design .....	122
5.2.3.2.	Case 1: analysis results when $S = 0$ .....	123
5.2.3.3.	Case 2: analysis results when $S = 1$ .....	125
	<b>DISCUSSION AND CONCLUSIONS.....</b>	<b>133</b>
	<b>REFERENCES .....</b>	<b>135</b>



## List of Tables

Table 2.1: Comparison between symmetric and asymmetric cryptography .....	8
Table 2.2: Image types vs. bit depth .....	12
Table 2.3: “Peppers” $256 \times 256$ image sizes in different formats .....	13
Table 2.4: Basic colors decomposition .....	14
Table 2.5: Statistical properties for standard images .....	16
Table 2.5: Statistical properties for standard images (Cont.) .....	17
Table 2.6: Correlation coefficients for “Peppers” $1024 \times 1024$ .....	19
Table 2.7: Entropy values for “Peppers” and “Lena” ( $1024 \times 1024$ ) .....	22
Table 2.8: NIST SP-800-22 statistical test [89].....	23
Table 2.9: NIST test results for encrypted “Peppers” and encrypted “Lena” .....	24
Table 2.10: Example of differential attacks results .....	25
Table 2.11: Mean square error values .....	26
Table 2.12: Maximum period LFSR feedback polynomials .....	32
Table 2.13: Step by step output of a 5-bit LFSR .....	33
Table 3.1: Correlation and differential attack measures for the simplified system .....	44
Table 3.2: NIST results for the simplified system .....	44
Table 3.3: Truth table for the multiplexing operation.....	45
Table 3.4: Analysis results for the proposed system.....	49
Table 3.5: Comparison to other related systems.....	49
Table 3.6: NIST results for the proposed system .....	49
Table 3.7: Wrong decryption results for one bit change in the key.....	50
Table 3.8: Correlation results .....	55
Table 3.9: Differential attack results.....	55
Table 3.10: Simplified system NIST results when encrypting Peppers image .....	56
Table 3.11: Shift values used for seven-fractals encryption .....	61
Table 3.12: Correlation and differential attack results for the Peppers image using two and seven fractals.....	61
Table 3.13: NIST results when encrypting Peppers image using two and seven fractals .....	62
Table 3.14: Wrong decryption for the Peppers image using seven fractals .....	64
Table 3.15: Results for colored images from USC-SIPI image database .....	65
Table 3.16: Comparison between the proposed system and other reported chaotic based systems .....	66
Table 3.17: Pixel correlation .....	69
Table 3.18: Entropy values.....	69
Table 3.19: Pixel correlation results for the three cases.....	72
Table 3.20: Entropy values results for the three cases.....	72
Table 3.21: NIST results for fractal 2 .....	73
Table 3.22: Analysis measures for encrypted image .....	74
Table 3.23: Entropy values for encrypted image.....	75
Table 3.24: NIST results for encrypted image .....	75
Table 4.1: Correlation coefficients of the proposed system.....	82
Table 4.2: Differential attack measures of the proposed system.....	83
Table 4.3: NIST test suite results of the proposed system .....	83
Table 4.4: MSE and entropy as measures of sensitivity analysis .....	84
Table 4.5: Comparison with other systems .....	85

Table 4.6: Analysis results of the proposed system.....	88
Table 4.7: NIST suite results of the proposed encryption system .....	88
Table 4.8: MSE and entropy as measures of sensitivity .....	89
Table 4.10: Comparison with other systems .....	90
Table 4.9: Results of encrypting different standard images .....	91
Table 4.11: Correlation coefficients for the source image and the encrypted image when $\alpha = 0.8$ and $c = 4$ .....	97
Table 4.12: Results for all correlation coefficients in the used ranges of $\alpha$ and $c$ .....	98
Table 4.13: Results for the differential attacks analysis .....	99
Table 5.1: Substitution only results (Peppers image, $L = 64$ ) .....	106
Table 5.2: Permutation only results (Peppers image, $L = 64$ ).....	106
Table 5.3: Proposed block cipher results (Peppers image, $L = 64$ ) .....	107
Table 5.4: NIST results for the encryption process .....	108
Table 5.5: Mean Square Error and entropy values .....	109
Table 5.6: Comparison with other systems .....	109
Table 5.7: Permutation matrix analysis results.....	117
Table 5.8: Adjacent pixels correlation results for Lena $256 \times 256$ .....	118
Table 5.9: Execution time ratios for the five algorithms .....	120
Table 5.10: Case 1 ( $S = 0$ ) encryption results for images with resolution $1024 \times 1024$ .....	124
Table 5.11: Case 2 ( $S = 1$ ) encryption results for Lena $1024 \times 1024$ .....	127
Table 5.12: Case 2 NIST results for encrypted Lena ( $1024 \times 1024$ ).....	128
Table 5.13: Case 2 NIST results for encrypted Peppers ( $1024 \times 1024$ ) .....	129
Table 5.14: Case 2 Mean Square Error and entropy results.....	131
Table 5.15: Permutation algorithms comparison for matrix size $M \times N$ .....	132

# List of Figures

Figure 2.1: Historical encryption devices (a) Scytale and (b) Engima machine .....	5
Figure 2.2: Block diagram for a typical cryptosystem.....	6
Figure 2.3: Block diagram for asymmetric algorithm .....	7
Figure 2.4: Block diagram for symmetric algorithms.....	8
Figure 2.5: Stream ciphering and block ciphering.....	9
Figure 2.6: Block cipher modes of operation (a) ECB mode, (b) CBC mode, (c) CFB mode, (d) OFB mode and (e) CTR mode.....	11
Figure 2.7: Encryption process .....	11
Figure 2.8: Typical image cryptosystem using symmetric-key.....	12
Figure 2.9: Typical image pixels representation.....	13
Figure 2.10: Pixel value representation.....	14
Figure 2.11: RGB color system .....	14
Figure 2.12: Statistical tests.....	18
Figure 2.13: Adjacent pixels in (a) “Peppers” image and (b) Encrypted “Peppers” .....	20
Figure 2.14: Histogram analysis .....	21
Figure 2.15: Sensitivity tests .....	24
Figure 2.16: Typical encryption system.....	27
Figure 2.17: 8 bit P-box.....	30
Figure 2.18: One round of an SPN .....	30
Figure 2.19: One round Fiestel network (a) classical Fiestel and (b) unbalanced fiestel .....	31
Figure 2.20: LFSR with maximum period connections (a) 5-bit and (b) 8-bit .....	32
Figure 2.21: Output of a 5-bit LFSR with maximum period $T = 31$ .....	33
Figure 2.22: Logistic map bifurcation diagram .....	34
Figure 2.23: Logistic map chaotic behavior when $\lambda = 3.999$ and $x_1 = 0.5$ .....	35
Figure 2.24: Bifurcation diagram for (a) sine map and (b) tent map.....	35
Figure 2.25: Lorenz attractor when $\sigma = 10, \rho = 28$ and $\beta = 83$ .....	36
Figure 2.26: Lorenz attractor .....	37
Figure 2.27: Rössler attractor .....	37
Figure 2.28: Encryption system design elements .....	41
Figure 3.1: Simplified system block diagram.....	43
Figure 3.2: System block diagram. ....	45
Figure 3.3: Generalized Feistel network internal structure. ....	46
Figure 3.4: S-box generation using an 8-bit LFSR initialized with the value 179. ....	47
Figure 3.5: System key details.....	47
Figure 3.6: Key values (a) for $M = 1$ and (b) $M = 4$ . ....	48
Figure 3.7: Peppers image and its encryption for (b) $M = 1$ and (c) $M = 4$ . ....	48
Figure 3.8: (a) Histogram and (b) Adjacent horz. pixels of the blue channel in the original Peppers image (top) and encrypted image for $M = 4$ (bottom). ....	50
Figure 3.9: Wrong decryption for the Peppers image. ....	50
Figure 3.10: Examples of fractal images.....	51
Figure 3.11: Mandelbulb creation using Eq. (17) for different values of $n$ (a) $n = 4$ , (b) $n = 6$ , (c) $n = 8$ and (d) $n = 10$ .....	54
Figure 3.12: Fractal images used in testing the proposed system; numbered 1 to 8 from left to right and from top to bottom .....	54
Figure 3.13: The simplified block diagram.....	55

Figure 3.14: Keystream generation using fractals.....	57
Figure 3.15: System block diagrams (a) encryption system and (b) decryption system.....	58
Figure 3.16: Key construction details.....	59
Figure 3.17: Example of key identification when using two fractals .....	59
Figure 3.18: Key length for different values of $K$ and $S$ when $M = 10$ ; black points are safe points where key length $\geq 128$ .....	60
Figure 3.19: (a) Peppers image, (b) encrypted Peppers image using two fractals, (c) encrypted Peppers image using seven fractals and (d) encrypted Peppers image using seven fractals after changing one pixel in the plain image .....	61
Figure 3.20: (a) Lena image, (b) encrypted Lena image using two fractals, (c) encrypted Lena image using seven fractals and (d) encrypted Lena image using seven fractals after changing one pixel in the plain image .....	61
Figure 3.21: Histogram for red, green and blue components of (a) Peppers image, (b) encrypted Peppers image using seven fractals, (c) Lena image and (d) encrypted Lena image using seven fractals .....	63
Figure 3.22: Wrong decryption of Peppers image (a) Test I, (b) Test II, (c) Test III and (d) Test V .....	64
Figure 3.23: SPN internal structure .....	68
Figure 3.24: Fractal images numbered 1 to 5 from left to right, top to bottom.....	68
Figure 3.25: Histogram analysis for (a) fractal 1 and (b) fractal 2 .....	69
Figure 3.26: The proposed block diagram of the PRKG based on fractals.....	70
Figure 3.27: Histogram analysis for the output stream when using fractal 2 in (a) Case A, (b) Case B and (c) Case C.....	71
Figure 3.28: The processed fractals after the different cases of post-processing .....	71
Figure 3.29: Block diagram for the encryption system.....	73
Figure 3.30: (a) Peppers image and (b) encrypted Peppers image. ....	74
Figure 3.31: Histogram analysis for (a) Peppers image and (b) encrypted image. ....	74
Figure 4.1: The conventional logistic, tent and sine maps. ....	77
Figure 4.2: The generalized logistic map when $\lambda = 3.99$ ; (a) function $f_g$ versus $x_n$ and $d$ when $c = 0.9$ , (b) chaotic output in the $c - d$ plane, and (c) the MLE values versus the $c - d$ plane. ....	78
Figure 4.3: The generalized tent map; (a) function $f_t$ versus $x_n$ and $b$ when $a = 1.3$ , (b) chaotic output in the $a - b$ plane when $r_t = 1.99$ , and (c) the MLE values versus the $r_t - b$ plane when $a = 1.3$ . ....	79
Figure 4.4: The generalized sine map; (a) function $f_s$ versus $x_n$ and $\beta$ when $\gamma = 1.1$ , $r_s = 0.9$ and $\alpha = 0.95$ , (b) chaotic output and (c) the MLE values in the $\beta - \gamma$ plane when $r_s = 0.9$ and $\alpha = 0.95$ . ....	80
Figure 4.5: Encryption block diagram based on generalized maps. ....	80
Figure 4.6: Encryption key. ....	81
Figure 4.7: The original Peppers image and its histograms and the second row is the encrypted TSG-image with its histograms. ....	82
Figure 4.8: Decrypted Lena image with one bit change in the key (a) Case I, (b) Case II, (c) Case III, (d) Case IV and (e) Case V .....	85
Figure 4.9: Encryption block diagram (left) and decryption block diagram (right). ....	86
Figure 4.10: Example utilization of the system key in constructing the parameters and initial conditions of the three maps.....	87
Figure 4.11: Histogram distributions for the original Lena image (first row) and its encrypted image (second row).....	88
Figure 4.12: Decrypted Lena image with one bit change in the key for (a) Case I, (b) Case II and (c) Case IV. ....	89

Figure 4.13: Strange attractor for the Lorenz system while fixing $c$ at 4; (a) $\alpha = 0.75$ (b) $\alpha = 0.8$ (c) $\alpha = 0.95$ (d) $\alpha = 1$ .....	94
Figure 4.14: Block diagram of the encryption process using the fractional-order Lorenz map.....	95
Figure 4.15: (a) Original image (Lena), and encrypted image at $c=4$ with (b) $\alpha = 0.75$ , (c) $\alpha = 0.8$ , and (d) $\alpha = 0.95$ .....	95
Figure 4.16: Histogram for red, green and blue components (a) of Lena (b) of the encrypted image shown in Fig. 4.15(c).....	96
Figure 4.17: Adjacent pixels values in horz., vert. and diag. directions in source (first row) and encrypted image (second row) for red component.....	97
Figure 4.18: Decryption with different values of $\alpha$ , (a) decrypted image with $\alpha = 0.799$ and $c = 4$ , $\Delta\alpha = -0.001$ , and (b) decrypted image with $\alpha = 0.801$ and $c = 4$ , $\Delta\alpha = +0.001$ .....	99
Figure 5.1: Block diagram of the chess-based chaotic block cipher .....	102
Figure 5.2: Block diagram of the decryption system.....	102
Figure 5.3: Flowchart for generating the permutation matrix .....	103
Figure 5.4: (a) Valid horse moves and (b) permutation matrix generated using the proposed algorithm .....	104
Figure 5.5: System key details.....	105
Figure 5.6: (a) Peppers image ( $1024 \times 1024$ ), (b) encrypted Peppers image, (c) Lena image ( $1024 \times 1024$ ) and (d) encrypted Lena image.....	107
Figure 5.7: Histograms for Peppers image (first row) and encrypted Peppers image using $L = 64$ (second row).....	107
Figure 5.8: Decrypted Peppers image with one bit change in the key (a) case I, (b) case II, (c) case III and (d) case IV.....	109
Figure 5.9: The permutation phase: (a) pixel processing indices, (b) an example of a permutation matrix $T$ and (c) new pixel locations after applying equation (56). .....	111
Figure 5.10: Permutation vectors mapping row and column indices.....	112
Figure 5.11: Modified horse move algorithm.....	114
Figure 5.12: Valid horse moves with start value = 1 and step value = 1. ....	114
Figure 5.13: Permutations effect for the five different techniques. ....	115
Figure 5.14: (a) ADOPM – $M/2$ and (b) ADBTAPav – $M/2$ . ....	116
Figure 5.15: (a) Lena. Scrambled Lena using: (b) Discrete Chaos, (c) Permutation Vectors, (d) Arnold's Cat Map, (e) Continuous Chaos and (f) Chess-based.....	118
Figure 5.16: The execution time ratios (a) for a single block of size $M$ and (b) for a complete “Lena” $1024 \times 1024$ with different block sizes $M$ . ....	120
Figure 5.17: Block diagrams of (a) encryption system and (b) decryption system. ....	121
Figure 5.18: Structure of the system key.....	122
Figure 5.19: Case 2 encryption and wrong decryption for Lena and Peppers images. ....	130

# Nomenclature

ADBTAP	The Average Distance Between Two Adjacent Pixels
ADOPM	The Average Distance One Pixel Moved
AES	Advanced Encryption Standard
CBC	Cipher Block Chaining Mode
CFB	Cipher Feedback Mode
CTR	Counter Mode
DCT	Discrete Cosine Transformation
DES	Data Encryption Standard
DSA	Digital Signature Algorithm
ECB	Electronic Codebook Mode
GFN	Generalized Feistel Network
IDEA	International Data Encryption Algorithm
IFS	Iterated Function Systems
IV	Initialization Vector
KG	Keystream Generator
LDE	Linear Diophantine Equation
LFSR	Linear Feedback Shift Register
LSB	Least Significant Bit
MAE	Mean Absolute Error
MLE	Maximum Lyapunov Exponent
MSE	Mean Square Error
NIST	The National Institute of Standards and Technology
NPCR	Number Of Pixels Change Rate
ODE	Ordinary Differential Equations
OFB	Output Feedback Mode
P-box	Permutation Box
PP	The Proportion Of Passing Sequences
PRKG	Pseudo Random Keystream Generator
PRNG	Pseudo Random Number Generator
PV	P-value Distribution
RSA	Rivest-Shamir-Adleman
S-box	Substitution Box
SPN	Substitution-Permutation Network
UACI	Unified Average Change Intensity
XOR	Modulo 2 Sum

# Abstract

Recently, the huge dependence on electronic communication has lead to an increased demand for data security in order to achieve privacy. The security of data transmission is a vital issue since it is easy to detect the information sent across the internet. Hence, a lot of research is performed in the field of data security in general and, consequently, image encryption arises as an important research field. A typical symmetric-key image encryption system usually consists of two main substitution and permutation phases to accomplish Shannon's confusion and diffusion properties. Therefore, this thesis introduces new encryption systems that utilize chaotic and non-chaotic generators in different designs of the aforementioned two phases.

Several stream-based image encryption systems are proposed and analyzed using chaotic as well as non-chaotic generators. Using non-chaotic generators, three stream-based systems are presented. The first system is designed by combining a Linear Feedback Shift Register (LFSR) with a generalized form of a Feistel-like structure in order to provide a strong keystream. The second system is based on fractal images where a set of fractal images is selected and processed in a form that achieves strong encryption. The third system proposes a different design of a pseudo random keystream generator based on fractal images.

In addition, two stream-based encryption systems are designed using chaotic generators. The first system is based on generalized forms of three discrete maps, which are the logistic map, the sine map and the tent map. By combining the three maps, a strong keystream is generated that helps in achieving the required encryption quality. The second system is based on the fractional-order Lorenz attractor. This system makes use of the extra degrees of freedom, which arise from the new fractional powers, and shows that the fractional order system exhibits a wider range in the new parameters that can achieve a chaotic behavior and helps in increasing the system key length and maintaining sensitivity to only one bit change.

On the other hand, two block-based image encryption systems are proposed and analyzed. The first system includes a novel chess-based permutation stage. The presented encryption algorithm is very sensitive to the input parameters, which helps in maintaining a very sensitive system key. The second system discusses five different algorithms for generating permutation matrices. The generated permutation matrices are, then, used in an encryption system in order to compare and evaluate the proposed permutation algorithms.

To evaluate the proposed encryption systems, the quality of the resulting ciphers is tested using adjacent pixels correlation coefficients, histogram distributions, differential attack measures and the NIST statistical test suite. Furthermore, sensitivity of the system key to one bit change is also examined using the mean square error and entropy values of the wrong decrypted images. Results achieved by the proposed cryptosystems are very promising and show great potential as compared to other systems in recent literature.