

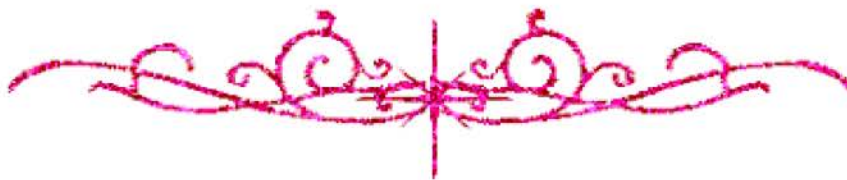
بسم الله الرحمن الرحيم



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شبكة المعلومات الجامعية التوثيق الالكتروني والميكرو فيلم



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جامعة عين شمس

التوثيق الإلكتروني والميكروفيلم

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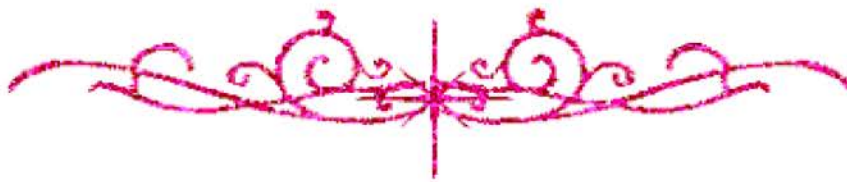
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لم ترد بالأصل



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SOME PROBLEMS IN NONLINEAR MECHANICS

Thesis

*Submitted for the Degree of
Doctor of philosophy*

by

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1996



سبحانك

لا علم لنا إلا ما علمتنا إنك أنت العليم الحكيم

- صدق الله العظيم -

سورة البقرة (آية ٢٥٥)

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*To My Dear Parents,
My Wife And My Childrens
(Dena & Ahmed)*

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