



AIN SHAMS UNIVERSITY
FACULTY OF ENGINEERING
STRUCTURAL ENGINEERING DEPARTMENT

**ANALYTICAL INVESTIGATION OF STATICALLY
INDETERMINATE FLEXURAL RC MEMBERS
STRENGTHENED BY PRESTRESSED STEEL AND FRP**

A Thesis
Submitted in Partial Fulfillment of the
Requirements for the Degree of

**MASTER OF SCIENCE
In
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STATEMENT

This thesis is submitted as partial fulfillment of the requirements for the degree of Master of Science in Civil Engineering (Structures), Faculty of Engineering, Ain Shams University.

The author carried out the work included in this thesis, and no part of it has been submitted for a degree or a qualification at any other scientific entity.

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