## A University text book

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#### PREFACE

The electronic systems and equipment such as radio transmitters, radio receivers, electronic exchangers, digital computers, ...etc., are generally composed of electronic circuits. Each circuit performs a predetermined function in the electronic system. Besides the conventional passive circuit elements, an electronic circuit contains electron devices.

The main duty of electron devices is amplification and switching. Moreover, they can act as controlled resistors and capacitors. Their inherent nonlinear electrical characteristics are extremely useful in signal processing.

A study of the electrical behavior of the electron devices is required not only to design them to meet specific terminal electrical characteristics, but also to apply them efficiently in electronic circuits.

Electronic devices can be classified in electron tubes and solid-state devices. In spite of the revolutionary advance in solid state devices since the invention of the transistor by W. Shockley in 1948, electron tubes are still dominant in applications where large power at high frequencies is necessary. This is because of the different nature of current conduction in vacuum tubes and in the solid materials.

In this book, the operating principles underlying the operation of junction devices an field effect devices are clearly presented. To facilitate the understanding the electron emission phenomenon and the electrical properties of semiconductors are also introduced. After studying this book thoroughly, the student would be able to develop himself alone in this important branch of science and engineering. The reader needs only background in elementary physics, mathematics and circuit theory for easy understanding the material of this book.

The author is indebted to Dr. Nabil M. Saleh et al., 1987, Professor of Electronics, Communications and Computer Department, Faculty of Engineering, Ain Shams University, for the critical review and for his continued interest and encouragement throughout the writing of this book.

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### FORWARD

It is with pleasure that I could introduce this book on Electron Devices, a subject that will continue to be one of the most important subject of modern electronics. For a number of years, I have been acquainted with Dr. A. Zekry's outstanding teaching and academic research achievement. His expert knowledge of electronic devices is reflected in this book. I wish to congratulate him for this project.

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## Chapter o

## 0.1 Review Of Some Physical Principles

In analyzing the properties of electron devices, we often deal with electrons. Thus, it is important to describe the electron and to know some facts about its motion under the influence of an electric field. In classical physics, the electron is considered as a particle, while in modern physics, wave properties are observed. In this chapter, we shall briefly review the basic physical principles of electron motion. Our purpose is to determine the conditions for validity of each model; the particle and wave models.

#### 0.1 The classical model

1

According to this model, the electron is a tiny negatively-charged particle. Its change q amounts to  $1.6 \times 10^{-19}$  coulomb and its mass at rest mo is  $9.1 \times 10^{-31}$  kg. Consequently, in order to determine the motion of the electron under the influence of different fields, the classical Newton's mechanics is used. If a force F acts upon a particle with mass m, it will be accelerated according to Newton's second law as follows,

$$\vec{F} = m\vec{a}$$
 (0.1) where  $\vec{a}$  is the acceleration of the particle.

The above law applies if the mass does not change with the velocity of the particle, i.e. constant. Otherwise, we have to use the general form of the Newton's equation of motion,

$$\vec{F} = \frac{d}{dt} (m\vec{v}) \tag{0.2}$$

where the product of mass, m, and velocity, v, is the momentum of the particle.

When the velocity of the electron approaches the velocity of light in free space, the relativistic variation of the mass with respect to the particle velocity must be taken into consideration. According to Lorentz and Einstein, this relation is given by,

$$m = \frac{m_o}{\sqrt{I - \left(\frac{v}{c}\right)^2}} \tag{0.3}$$

where v is the velocity of the particle, c is the velocity of light = $3 \times 10^8$  m/s, and m<sub>o</sub> is the mass at rest.

## 0.2 Motion of an electron in vacuum under the influence of an electric field $\boldsymbol{E}$

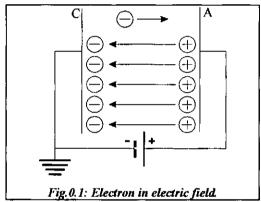
One practical way to produce an electric field is to apply a battery on two metalic electrodes, which are situated in vacuum as shown in Fig.0.1. If an electron is present at the position x, it will move in the positive x-direction, in the opposite direction of the electric field. We are interested now to get a relation between the velocity of the electron at any position x, and the electric potential at the same point.

We shall consider the electron as a particle. Hence, we can write:

$$\vec{F} = m \frac{d\vec{v}}{dt}$$

Multiplying both sides by dx, scalarily then one obtains:

$$\vec{F}.d\vec{x} = m\frac{d\vec{v}}{dt}.d\vec{x} \qquad (0.4)$$



By definition, the force acting on the electron due to the electric field  $\vec{E}$  is given by:

$$\vec{F} = -q\vec{E} \tag{0.5}$$

Substituting (0.5) in (0.4), we get:

$$q(-\vec{E}.d\vec{x}) = m\vec{v}.d\vec{v} \tag{0.6}$$

We know that the incremental potential difference  $dV = -\vec{E}.d\vec{x}$ , then from eqn. (0.6), we get: q.dv = mvdv

Integrating this equation from x=0 to any point x, we obtain:

$$q \int_{v(0)}^{v(x)} dV = \left(\frac{mv^2}{2}\right]_{v(0)=0}^{v(x)}$$

Therefore:

$$q[V(x)-V(0)] = \left[\frac{m}{2}v^{2}(x) - \frac{m}{2}v^{2}(0)\right]$$
 (0.7)

The kinetic energy, **K.E.**, of a particle with mass m and velocity v equals  $mv^2/2$ , while the potential energy, **P.E.**= charge  $\times$  potential.

The above equation then can be rewritten in the form:

$$P.E.\Big|_{x=0} - P.E.\Big|_{x} = K.E.\Big|_{x} - K.E.\Big|_{x=0}$$
 (0.8)

Equation (0.7) states that the decrease in potential energy of the electron is equal to the increase in its kinetic energy, which means that the electrostatic field is conservative.

Assuming that the potential of the plate C is equal to zero, and the electron starts at rest at x=0, then eqn.(0.7) reduces to the simple relation,

$$q.V(x) = \frac{mv^{2}(x)}{2}$$

$$V(x) = \sqrt{\frac{2e}{m}V(x)}$$
(0.9)

This relation between the velocity of a charged patricle and its potential is of a great importance for determining the electrical characteristic of vacuum tubes as we shall see in chapter 3.

#### 0.3 Relativity theory

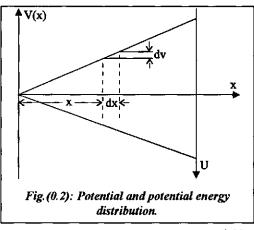
We see easily from eqn.(0.9) that as the potential V is raised, the velocity of the particle v increases, and it can approach the velocity of light in free space. Here, the classical Newton's mechanics does not hold any longer. Instead, the relativistic mechanics founded by Einstein must by used. The relativity theory states that the energy equivalence of a mass m is equal to the product of this mass and the square of the velocity of light,

$$W = m C^2$$

Applying the above law on our problem, the energy equivalence W(0) of electron with a mass  $m_0$  at rest is given by the relation:

$$W(0) = m_o C^2 (0.10)$$

Now, if an electron falls down in the potential energy hill, Fig. (0.2), it acquires kinetic energy, its velocity will be increased. This means that the electron gains kinetic energy from the electric field. Its energy equivalence at any point x, greater than zero, will be higher than that at rest. Hence, the new energy equivalence of the electron at point x can be expressed by:



$$W(x) = m C^2$$

(0.11)

With m greater than m<sub>o</sub>. Notice here that the velocity of light is time-invariant, i.e. it does not depend on time.

Since the electrostatic field is conservative, as previously proved in section 0.2, then the increase in the electron energy is equal to the mechanical work done by the electric field, we get finally the energy balance:

$$qV = mc^2 - m_e c^2 \tag{0.12}$$

Combining eqn. (0.12) with Lorentz-Einstein eqn. (0.3), we can get the actual velocity v of the particle.

### 0.4 Second model of the Electron

#### 0.4.1 Wave properties of the electron

In many experiments in physics, it was found that the electrons show wave properties such as diffraction and interference. The motion of an electron in this case can be defined by applying the laws of the wave mechanics. The founders of wave mechanics are three young scientists, de Broglie, Heisenberg and Schroedinger. They won Nobel prize for physics for

their contribution. De Broglie postulated that the wave length,  $\lambda$ , of a particle wave is inversely proportional to its mass m and velocity v.

$$\lambda = \frac{h}{mv} = \frac{h}{p} \tag{0.13}$$

where h is Planck's constant =  $6.625 \times 10^{-36}$  J. sec., and P is the momentum of the particle.

This postulate is very important in wave mechanics. Specifically with the help of this equation, we can determine whether a moving particle behaves actually as a particle or as a wave. That is if  $\lambda$  is much smaller than the physical dimensions of the particle and the space in which the particle moves, then we shall measure only the particle properties, and we can use the classical mechanics to describe its motion.

On the other side, if  $\lambda$  is in the order of the physical dimensions of particle and the space in which the particle moves, such as the motion of an electron in an atom or in crystal, we have to use the wave mechanics to detect the physical behavior of the system.

### 0.4.2 Schroedinger Equation

Schroedinger equation represents the basis of the wave mechanics, as Newton's equation in the classical mechanics. The time independent Schroedinger equation can be written in the form:

$$\left(-\frac{\hbar^2}{2m}\nabla^2 + U\right)\Psi = W\Psi \tag{0.14}$$

with 
$$\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \equiv \text{Laplace operator, and}$$

$$\hbar = \frac{h}{2\pi}$$

where U(x,y,z) is the potential energy, W is the total energy of the electron, m is its mass, and  $\Psi$  is the wave function to be determined in space by solving the above differential equation with appropriate boundary conditions.  $\Psi$  describes totally the motion of the electron in the potential field U. The