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بالرسالة صفحات

لم ترد بالأصل

HOSSAM MAGHRABY

Fractional Calculus Stability, Fractional-Oscillators, and Fractional-Filters: Theories and Applications.

By

Eng. Ahmed Gomaa Ahmed Radwan

A Thesis submitted to the
Faculty of Engineering at Cairo University
In partial Fulfillment of the Requirements
For the Degree of
DOCTOR OF PHILOSPHY
In
Engineering Mathematics

Faculty of Engineering – Cairo University
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November 2006

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