



شبكة المعلومات الجامعية
التوثيق الإلكتروني والميكروفيلم

بسم الله الرحمن الرحيم



MONA MAGHRABY



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جامعة عين شمس

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AIN SHAMS UNIVERSITY
FACULTY OF ENGINEERING
STRUCTURAL ENGINEERING DEPARTMENT

**Moment Redistribution in Continuous RC Elements Top
Strengthened with CFRP and Steel Plates**

A thesis submitted in partial fulfillment of the
requirements for the degree of

Doctor of Philosophy
in Civil Engineering (Structural)
by

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Master of Science in Civil Engineering (Structural)
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Cairo – (2020)



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STATEMENT

This thesis is submitted to Ain Shams University, Cairo, Egypt, for the degree of Doctor of Philosophy in Civil Engineering (Structural).

The work included in this thesis was carried out by the author at the reinforced concrete lab, Structural Engineering department, Faculty of Engineering, Ain Shams University.

No part of this thesis has been submitted for a degree or qualification at any other University or Institute.

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Amr Mohamed Ibrahim Mostafa

Dedication

*I dedicate this thesis to my late father **Mohamed Ibrahim**, for raising me on the value of insistence and determination, setting an example of whom I would be so proud to be and sacrificing his comfort to provide the perfect atmosphere for me and my brothers.*

*I am heavily indebted to my loving **mother**, for inundating me with her infinite love and care, motivating me to chase my dreams, her continuous help and praying for me to accomplish success in my life.*

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