

بسم الله الرحمن الرحيم

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DEVELOPMENT OF FUZZY LOGIC BASED MODEL PREDICTIVE CONTROL FOR PATH TRACKING OF AUTONOMOUS VEHICLE

By Nada Awad Sadek Mogoda

A Thesis Submitted to the
Faculty of Engineering at Cairo University
in Partial Fulfillment of the
Requirements for the Degree of
MASTER OF SCIENCE

in

Electrical Power and Machines Engineering

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Under the Supervision of

Kamel	Dr. Manmoud Monamed Elnaggar
Professor at	Assistant Professor at
Electrical Power and Machines Department	Electrical Power and Machines Department
Faculty of Engineering, Cairo	Faculty of Engineering, Some
University	University

Dr. Ahmed Abdel Nasser Lasheen

.....

Assistant Professor at
Electrical Power and Machines Department
Faculty of Engineering, Other
University

FACULTY OF ENGINEERING, CAIRO UNIVERSITY GIZA, EGYPT 2022

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Approved by the Examining Committee	
Prof. Dr. Ahmed Mohamed Ahmed Kamel,	(Thesis Main Advisor)
Prof. Dr. Abdel Latif Mohamed Ragaei Elsl	hafei , (Internal Examiner)
of Dr. Adal Abdal Manaam Elsamahy	(External Examinar)

- Professor at Helwan University

(External Examiner)

Engineer's Name: Nada Awad Sadek Mogoda

Date of Birth: 27/9/1994 **Nationality:** Egyptian

E-mail: Nadaawad.da20@gmail.com

Phone: 01060711230

Address: 179 fifth district, El Sheikh Zayed

Registration Date: 1/10/2017 **Awarding Date:**/2022 **Degree:** Master of Science

Department: Electrical Power and Machines Engineering

Supervisors:

Prof. Ahmed Mohamed Ahmed Kamel Dr. Mahmoud Mohamed Elnaggar Dr. Ahmed Abdelnasser Lasheen

Examiners:

Prof. Ahmed Mohamed Ahmed Kamel (Thesis main

advisor)

Prof. Abdel Latef Mohamed Ragaei Elshafei (Internal

examiner)

Prof. Adel Abdel Menaam Elsamahy (External

examiner)

(Helwan University)

Title of Thesis:

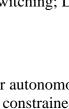
Development of Fuzzy Logic Based Model Predictive Control for Path Tracking of the Autonomous Vehicle

Key Words:

Autonomous Vehicles; Model Predictive Control; Fuzzy Logic Switching; Linear Quadratic Regulator; Kalman Filter.

Summary:

The present thesis explains a path tracking control technique for autonomous ground vehicles. It develops a control technique based on the linear constrained model predictive control for the autonomous vehicle to follow a given path. The system architecture includes the; path planning model, fuzzy switching system, path tracking controller, and the nonlinear vehicle model. A detailed vehicle model is developed with three degrees of freedom and the Pacejka tires model. The fuzzy logic switching module is used for online switching between the linearized vehicle models. Further approaches are developed on the vehicle model, such as the discrete linear quadratic regulator as a tracking controller and the Kalman filter.



Disclaimer

I hereby declare that this thesis is my own original work and that no part of it has been submitted for a degree qualification at any other university or institute.

I further declare that I have appropriately acknowledged all sources used and have cited them in the references section.

Name: Date: ../../2022

Signature:

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Nomenclature

Symbols:

$F_{\mathcal{Y}}$	Lateral force of the vehicle
F_{χ}	Longitudinal force of the vehicle Lateral stiffness of the tires
C_{α}	Longitudinal stiffness of the tires
C_{σ}	
α	Side slip angle
R_{eff}	Effective wheel radius,
ω	Angular velocity
V_{x}	Linear velocity
<u>μ</u>	Friction coefficient
F_{Z}	Vertical load of the vehicle
m	Mass of the vehicle
g	Gravitational acceleration
X	Coordinate system in the reference planar frame in the x direction
Y	Coordinate system in the reference planar frame in the y direction
φ	Heading angle
β	Slip angle
v	Magnitude of the velocity vector.
l_r	Rear distances from the center of mass.
l_f	Front distances from the center of mass
δ	Steering angle
E	Force generated at the wheel contact surface with the ground in the x-
$F_{x,i}$	axis, where <i>i</i> indicates front or rear wheel
$F_{y,i}$	Force generated at the wheel contact surface with the ground in the y-
1 y,l	axis direction, where <i>i</i> indicates front or rear wheel
V_g	Vehicle speed at the car center of gravity
α_f	Vehicle front slip angle
I_{Z}	Moment of inertia around the z-axis
$V_{wx,f}$	Linear velocities of the wheels front and rear, in the x-axis direction
$V_{wy,f}$	Linear velocities of the wheels front and rear, in the y-axis direction
χ̈́	Velocity component in the vehicle frame in the x-axis direction
ý	Velocity component in the vehicle frame in the y-axis direction
$F_{x,r}$	Forces in the x directions for the rear wheels
F_{yf}	Forces in the y directions for the front wheels
v_x	Longitudinal velocity,
v_y	Lateral velocity,
r	Yaw rate
a_x	Longitudinal accelerations of the vehicle
a_{ν}	Lateral accelerations of the vehicle
J_z	Vehicle yaw inertia
b_f and b_r	Front and rear track width.
ν_f and ν_r	1 fort and fear track within

$\begin{array}{c} c_W & \text{Aerodynamic drag coefficient} \\ \rho & \text{Air density} \\ A & \text{Frontal area of the vehicle} \\ \lambda_i & \text{Slipe ratio of the ith wheel} \\ F_{zi} & \text{Normal force of the ith wheel} \\ h & \text{Height of the center of gravity of the vehicle from the ground} \\ \omega_i & \text{Angular velocity of the ith wheel} \\ x & \text{State space vector} \\ u & \text{State space output vector} \\ y & \text{State space output vector} \\ Q_i \text{ and } C_i & \text{Discrete state space model matrices} \\ Q_i \text{ and } R_i & \text{MPC tracking controller design parameters} \\ K_{dlqr} & \text{Gain matrix of the DLQR} \\ N_p & \text{Prediction horizon of the MPC} \\ N_c & \text{Control horizon of the MPC} \\ X_{ref_1} & \text{Reference states at sample time } i \\ u_{ref_1} & \text{System inputs reference signals} \\ N & \text{Number of the Laguerre terms} \\ a & \text{Pole of the discrete-time Laguerre network} \\ \eta & \text{Laguerre parameter vector} \\ u_{min} \text{ and } & \text{Minimum and the maximum input values} \\ u_{max} & \\ \Delta u_{min} & \text{and } & \text{Minimum and the maximum values of the rate of change of the inputs} \\ \lambda_{max} & \\ R_L & \text{Optimization problem input increments} \\ L(i) & \text{Laguerre functions at time sample i} \\ N_S & \text{States number} \\ \omega_{min} & \text{Minimum value of the angular velocity} \\ \end{array}$		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$V_{\rm w1}$	Speed of the vehicle wheel number 1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	c_W	Aerodynamic drag coefficient
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	ho	Air density
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	A	Frontal area of the vehicle
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	F_{zi}	Normal force of the ith wheel
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	h	Height of the center of gravity of the vehicle from the ground
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	ω_i	Angular velocity of the ith wheel
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	x	State space vector
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	и	State space input vector
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	У	State space output vector
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	A_i , B_i , and C_i	Discrete state space model matrices
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	N_S	
Maximum value of the angular velocity	ω_{min}	
770000	ω_{max}	Maximum value of the angular velocity
δ_{min} Stearing angle minimum value		Stearing angle minimum value
δ_{max} Stearing angle maximum value	δ_{max}	
$\Delta\delta$ Rate of change of the steering angle	Δδ	
$\Delta \delta_{max}$ Maximum value of the rate of change of the steering angle	$\Delta\delta_{max}$	
$\Delta \delta_{min}$ Minimum value of the rate of change of the steering angle		Minimum value of the rate of change of the steering angle