



شبكة المعلومات الجامعية  
التوثيق الإلكتروني والميكرو فيلم

# بسم الله الرحمن الرحيم



**MONA MAGHRABY**



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التوثيق الإلكتروني والميكروفيلم



# شبكة المعلومات الجامعية التوثيق الإلكتروني والميكروفيلم



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# جامعة عين شمس

## التوثيق الإلكتروني والميكروفيلم

### قسم

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### يجب أن

تحفظ هذه الأقراص المدمجة بعيدا عن الغبار



**MONA MAGHRABY**



Cairo University

**DESIGNING OF FUZZY LOGIC BASED COMPUTED TORQUE  
CONTROLLERS FOR 6 DEGREE OF FREEDOM ROBOTIC  
MANIPULATOR**

By

**Asmaa Mohamed Abd El-Star**

A Thesis Submitted to the  
Faculty of Engineering at Cairo University  
in Partial Fulfillment of the  
Requirements for the Degree of  
**MASTER OF SCIENCE**

In  
**ELECTRICAL POWER AND MACHINES ENGINEERING**

FACULTY OF ENGINEERING, CAIRO UNIVERSITY  
GIZA, EGYPT  
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DESIGNING OF FUZZY LOGIC BASED COMPUTED TORQUE  
CONTROLLERS FOR 6 DEGREE OF FREEDOM ROBOTIC MANIPULATOR

**Key Words:**

Robotic manipulators; Computed torque control; Fuzzy control

**Summary:**

Three different control strategies have been developed to control the 6-degree of freedom. Robot manipulator such that it can track the required trajectories. The first is based on the feedback linearization of the manipulator and controller via using a nonlinear control law. This is called a computed-torque-controller (CTC). The second is a Fuzzy controller. The third is a hybrid controller from the first and the second ones. The developed controllers are tested in different cases of uncertainties in the nonlinearity of the manipulator. The third

controller has proved its superiority over the other two controllers in case of the motion is either from point to point or oscillatory with small frequency.

## **Disclaimer**

I hereby declare that this thesis is my own original work and that no part of it has been submitted for a degree qualification at any other university or institute.

I further declare that I have appropriately acknowledged all sources used and have cited them in the references section.

Name: Asmaa Mohamed Abd El-star

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# **Dedication**

To my mother and my husband. Without whom this work would not have been completed.

## **Acknowledgments**

First of all, thanks god for helping me throughout my whole life. All praise is due to Allah who guided me to this.

I would like to thank Prof. Dr. Ahmed Kamel. He has been very supportive and has always provided me with the encouragement and advice to finish my work. I think that he has a serious personality. I learned great lessons from this serious and organized personality.

I also would like to thank Dr. Ahmed Lasheen who has treated me as step brother. During his supervision he has done great effort to make this work. As a result of his sincere and devoted efforts, this work becomes in this form.

To the candle that lights the path of my life, for my mother who built me to be as I am, thesis dedication is not enough to thank her.

I would like to thanks my husband. He has encouraged me in my work and has dedicated all his love, life and care for me.

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