



شبكة المعلومات الجامعية
التوثيق الإلكتروني والميكروفيلم

بسم الله الرحمن الرحيم



MONA MAGHRABY



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شبكة المعلومات الجامعية التوثيق الإلكتروني والميكروفيلم



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جامعة عين شمس

التوثيق الإلكتروني والميكروفيلم

قسم

نقسم بالله العظيم أن المادة التي تم توثيقها وتسجيلها
علي هذه الأقراص المدمجة قد أعدت دون أية تغييرات



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تحفظ هذه الأقراص المدمجة بعيدا عن الغبار



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Fixed points on proximinal sets and one step iterative scheme

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- N. Faried, H. Abd El Ghaffar and S. Hamdy, “Fixed point theory for finite ϕ -weak contraction functions”, Global Journal of Pure and Applied Mathematics, ISSN 0973-1768, Vol. 12, **2016**, No. 6, pp. 5149-5155.
- N. Faried, H. Abd El Ghaffar and S. Hamdy, “Fixed point theory for three ϕ -weak contraction functions”, J. Appl. Computat. Math., ISSN: 2168-9679, Vol 6, **2017**, Issue 1, pp. 338.
- N. Faried, H. Abd El Ghaffar and S. Hamdy, “Common Fixed Point for Two Multivalued Mappings on Proximinal Sets in Regular Modular Metric Space”, Pure and Applied Mathematics Journal, 9(4), 74-83, **2020**.

SUMMARY

