



شبكة المعلومات الجامعية  
التوثيق الإلكتروني والميكروفيلم

# بسم الله الرحمن الرحيم



**HANAA ALY**



شبكة المعلومات الجامعية  
التوثيق الإلكتروني والميكروفيلم



## شبكة المعلومات الجامعية التوثيق الإلكتروني والميكروفيلم



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# جامعة عين شمس التوثيق الإلكتروني والميكروفيلم

## قسم

نقسم بالله العظيم أن المادة التي تم توثيقها وتسجيلها  
علي هذه الأقراص المدمجة قد أعدت دون أية تغييرات



## يجب أن

تحفظ هذه الأقراص المدمجة بعيدا عن الغبار



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Cairo University

NUMERICAL ANALYSIS OF STONE COLUMNS IN  
LIQUEFIABLE SOIL

By

**Adham Gamal Diaeldin Abdelrazek**

A Thesis Submitted to the  
Faculty of Engineering at Cairo University  
in Partial Fulfillment of the  
Requirements for the Degree of  
**MASTER OF SCIENCE**  
in  
**Civil Engineering - Public Works**

**FACULTY OF ENGINEERING, CAIRO UNIVERSITY**

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**Title of Thesis:**

NUMERICAL ANALYSIS OF STONE COLUMNS IN LIQUEFIABLE SOIL

**Key Words:**

Stone Column; Numerical Modelling; Liquefaction; PM4Sand; UBC3D-PLM.

**Summary:**

This research examines the behaviour of stone columns in liquefiable soils. Stone column in-situ stiffness and the improvement in the field's liquefaction resistance are not directly related to results of plate load tests. Two series of parametric studies program compromise static and dynamic analyses conducted using a 2D finite element model to investigate this relation. The study addressed the effect of stone columns on liquefiable soils, also, it studied the stone columns behaviour in such soils and estimate the degree of soil improvement against liquefaction. The study performs a design curve that relates the interpreted column stiffness with the reduction in shear stresses.

## **Disclaimer**

I hereby declare that this thesis is my own original work and that no part of it has been submitted for a degree qualification at any other university or institute.

I further declare that I have appropriately acknowledged all sources used and have cited them in the references section.

Name: Adham Gamal Diaaeldin Abdelrazek

Signature:

Date:

## **Dedication**

*To: My Family*

*&*

*To: Prof. Dr Sherif Wissa (Kind Soul)*

## **Acknowledgments**

First, Thanks for God for all things given throughout my entire life and for giving the ability to proceed in my life, studies till the moment and more.

The author gratefully acknowledges the technical support of this study by Dar Al-Handasah (Shair and Partners) Company for allowing and supporting the use of all Plaxis software.

I would like to express my sincere gratitude to my advisor Dr. Sherif Adel Akl Associate Professor of Geotechnical Engineering and foundations, Faculty of Engineering, Cairo University, for the continuous support of my master study and research, for his patience, motivation, enthusiasm, and immense knowledge. His guidance helped me in all the time of research and writing of this thesis. I could not have imagined having a better advisor and mentor for my master study.

Foremost, I would like to thank my godfather of geotechnical engineering, Prof. Dr. Sherif Wissa for the encouragement, patient guidance advice, motivation, enthusiasm, and immense knowledge that has provided throughout the time of research. Also, I would like to present this study for his kind soul.

I place on record, my sincere thank you to all my friends and Dar Colleagues for their continuous encouragement, motivating me to do my thesis.

Finally, my gratitude to my beloved family for all their help and encouragement through every step in my life and my studies.

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