

بسم الله الرحمن الرحيم





شبكة المعلومات الجامعية التوثيق الالكتروني والميكرو فيلم



جامعة عين شمس

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A Generalization of the Moyal Distribution

A Thesis submitted in Partial Fulfillment of the
requirement for the Master Degree in Science in
Mathematical Statistics

By

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